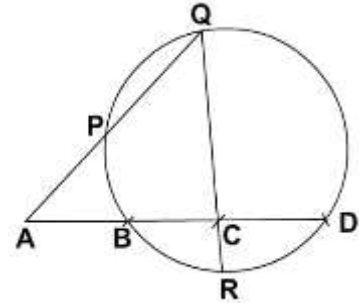


5. In the adjoining figure,
 $AB = BC = CD$.

P is the midpoint of AQ .

If $CR = 4$, $QC = 12$, then PQ is equal to

- a) $4\sqrt{3}$ b) $6\sqrt{3}$
 c) $8\sqrt{3}$ d) $2\sqrt{3}$

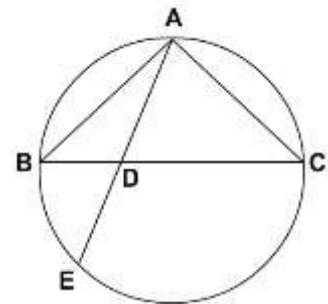


6. In the adjoining figure, A is the midpoint of the arc BAC .

Given that $AB = 15$ and $AD = 10$.

Then the value of AE is

- a) 22 b) 23
 c) 22.5 d) 23.5



7. The number of real numbers x which satisfy the equation $\frac{8^x + 27^x}{12^x + 18^x} = \frac{7}{6}$ is

- a) 1 b) 2 c) 0 d) 4

8. a, b are real numbers such that $2a^2 + 5b^2 = 20$. Then the maximum value of $a^4 b^6$ is

- a) 256 b) 1024 c) 1262 d) 16

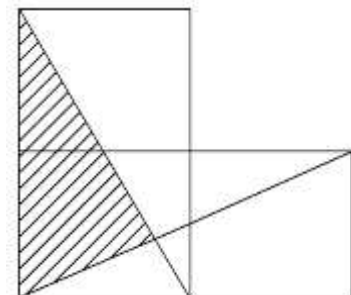
9. The number of ordered pairs (x, y) of integers such that $x - y^2 = 4$ and $x^2 + y^4 = 26$ is

- a) 4 b) 3 c) 2 d) 1

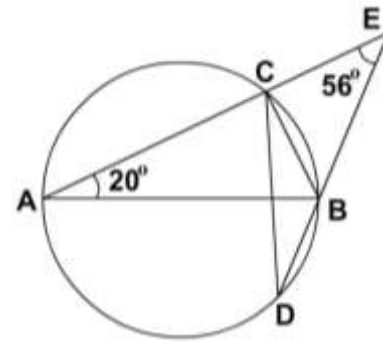
10. In the adjoining figure, three equal squares are placed. The squares are unit squares.

The area of the shaded region (in cm^2) is

- a) $\frac{5}{4}$ b) $\frac{4}{5}$
 c) $\frac{3}{2}$ d) $\frac{3}{4}$



11. In the adjoining figure, AB is a diameter of the circle. Given $\angle BAC = 20^\circ$, $\angle AEB = 56^\circ$. Then the measure (in degrees) of $\angle BCD$ is



- a) 12 b) 10
c) 14 d) 16

12. The number of ordered pairs $((m, n))$ of integers such that $1 \leq m, n \leq 100$ and $m^n n^m$ leaves a remainder 1 when divided by 4 is

- a) 2250 b) 1000 c) 1125 d) 1250

13. The number of ordered pairs of positive integers (x, y) satisfying the equation $x^2 + 4y = 3x + 16$ is

- a) 1 b) 2 c) 3 d) 4

14. The algebraic expression $(a + b + ab + 2)^2 + (a - ab + 2 - b)^2 - 2b^2(1 + a^2)$ reduces to

- a) $4(a + 2)^2$ b) $2(a + 2)^2 + 4ab^2$ c) $(a - 2)^2$ d) $2(a - 2)^2 + 4ab^2$

15. The sum of $(1 \times 4) + (2 \times 7) + (3 \times 10) + (4 \times 13) + \dots$ 49 terms is equal to

- a) 122500 b) 116800 c) 11800 d) 117600

Section B

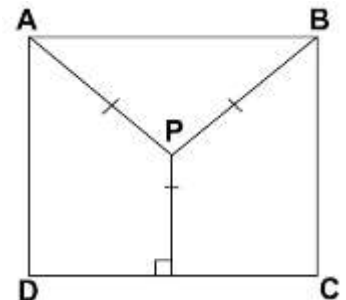
16. If the equations $x^3 + ax + 1 = 0$ and $x^4 - ax^2 + 1 = 0$ have a common root, then the value of a^2 is _____.

17. If a, b, c, d are positive reals such that $abcd = 1$ then the maximum value of $a^2 + b^2 + c^2 + d^2 + ab + ac + ad + bc + bd + cd$ is _____.

18. The sum of all natural numbers 'n' for which $n(n+1)$ is a perfect square is _____.

19. P is a point inside the square $ABCD$ such that $PA = PB =$ Distance of P from CD .

The ratio of the areas of the triangle PAB to the area of the square $ABCD$ is $\frac{m}{n}$ where m, n are relatively prime integers. Then the value of $m + n =$ _____.



20. The sum of roots of the simultaneous equations

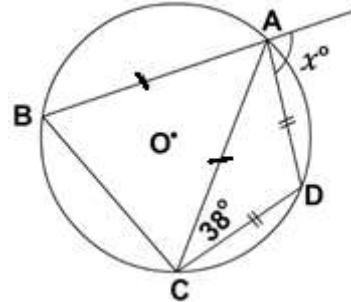
$$\sqrt[y]{4^x} = 32^x \sqrt{8^y}, \quad \sqrt[y]{3^x} = 3 \sqrt[y]{9^{1-y}} \quad \text{is } \underline{\hspace{2cm}}.$$

21. If $2\sqrt{3+\sqrt{5-\sqrt{13+\sqrt{48}}}} = \sqrt{a} + \sqrt{b}$ where a, b are natural numbers, then the value of $a + b$ is $\underline{\hspace{2cm}}$.

22. In the adjoining figure, $\angle ACD = 38^\circ$.

Then the measure (in degrees) of

angle x is $\underline{\hspace{2cm}}$



23. If $\frac{a}{b+c} + \frac{c}{a+b} = \frac{2b}{c+a}$ (where $a+b, b+c, c+a, a+b+c$ are all not zero), then the numerical value of $\frac{a^2+c^2}{b^2}$ is $\underline{\hspace{2cm}}$.

24. The geometric and arithmetic means of two positive numbers are respectively 8 and 17. The larger among the two numbers is $\underline{\hspace{2cm}}$.

25. The number of two-digit numbers in which the tens and the units digit are different and odd is $\underline{\hspace{2cm}}$.

26. The value of $(5\sqrt[3]{4} - 3\sqrt[3]{1/2})(12\sqrt[3]{2} + \sqrt[3]{16} - 2\sqrt[3]{2})$ is equal to $\underline{\hspace{2cm}}$.

27. If $\frac{xy}{x+y} = 1, \frac{yz}{y+z} = 2, \frac{zx}{z+x} = 3$, then the numerical value of $15x - 7y - z$ is $\underline{\hspace{2cm}}$.

28. The sum of all natural numbers which satisfy the simultaneous *inequations* $x+3 < 4+2x$ and $5x-3 < 4x-1$ is $\underline{\hspace{2cm}}$.

29. In an increasing geometric progression (with 1st term a and n^{th} term t_n), the difference between the fourth and the first term is 52 and the sum of

the first three terms is 26. Then the numerical value of $\frac{t_{2024}}{t_{2023}} + \frac{a^{2024}}{a^{2023}}$ is $\underline{\hspace{2cm}}$

30. The base of a triangle is 4 units less than the altitude drawn to it. The area of the triangle is 96 (unit²). The ratio of the base to height is $\frac{p}{q}$ where p, q are relatively prime to each other. Then the value of $p+q$ is $\underline{\hspace{2cm}}$.