

Matrix JEE Academy

# JEE-MAIN 2016 TEST PAPER WITH SOLUTION Held on 03 April 2016

#### PART-A - PHYSICS

1. A particle performs simple harmonic motion with amplitude A. Its speed is trebled at the instant that it is a

distance  $\frac{2A}{3}$  from equilibrium position. The new amplitude of the motion is :

(1) 
$$A\sqrt{3}$$
 (2)  $\frac{7A}{3}$  (3)  $\frac{A}{3}\sqrt{41}$  (4)  $3A$ 

Sol. 
$$\mathbf{v} = \omega \sqrt{\mathbf{A}^2 - \left(\frac{2}{3}\mathbf{A}\right)^2}$$
 (1)

$$3\mathbf{v} = \omega \sqrt{\left(\mathbf{A'}\right)^2 - \left(\frac{2}{3}\mathbf{A}\right)^2} \tag{2}$$

Divide the two equations.

$$\mathbf{A'} = \frac{7}{3}\mathbf{A}$$

Sol.

2. For a common emitter configuration, if  $\alpha$  and  $\beta$  have their usual meanings, the uncorrect relationship between  $\alpha$  and  $\beta$  is :

(1) 
$$\alpha = \frac{\beta}{1+\beta}$$
 (2)  $\alpha = \frac{\beta^2}{1+\beta^2}$  (3)  $\frac{1}{\alpha} = \frac{1}{\beta} + 1$  (4)  $\alpha = \frac{\beta}{1-\beta}$   
 $\alpha = \frac{I_c}{I_e}$   
 $\beta = \frac{I_c}{I_b}$   
 $I_e = I_b + I_c$   
 $\frac{I_e}{I_c} = \frac{I_b}{I_c} + 1$   
 $\therefore \frac{1}{\alpha} = \frac{1}{\beta} + 1$ 

A student measures the time period of 100 oscillations of a simple pendulum four times. The data set is 90 s,
 95 s and 92 s. If the minimum division in the measuring clock is 1 s, then the reported mean time should be :

(1) 
$$92 \pm 1.8 \text{ s}$$
 (2)  $92 \pm 3 \text{ s}$  (3)  $92 \pm 2 \text{ s}$  (4)  $92 \pm 5.0 \text{ s}$   
Sol.  $< T > = \frac{90 + 91 + 95 + 92}{4} = 92$   
 $\Delta T_1 = |90 - 92|, \ \Delta T_2 = |91 - 92|, \ \Delta T_3 = |95 - 92|, \ \Delta T_4 = |92 - 92|$ 



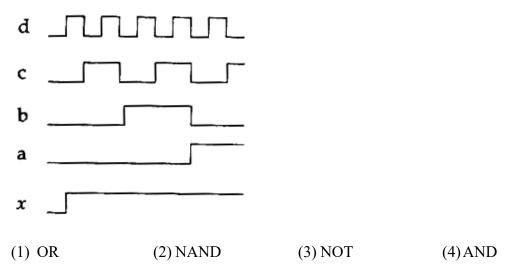
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 $<\Delta T>=1.5$ 

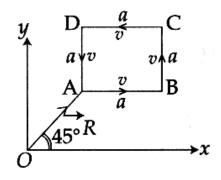
Since least count of the measuring clock is 1 second therefore,

 $T = 92 \pm 2$ 

4. If a, b, c, d are inputs to a gate and x is the output, then, as per the following time graph, the gate is :



- Sol. Output represents OR gate.
- 5. A particle of mass m is moving along the side of a square of side 'a', with a uniform speed v in the x-y plane as shown in the figure :



Which of the following statements is false for the angular momentum  $\vec{L}$  about the origin?

- (1)  $\vec{L} = m\upsilon \left[\frac{R}{\sqrt{2}} + a\right]\hat{k}$  when the particle is moving from B to C
- (2)  $\vec{L} = \frac{m0}{\sqrt{2}} R\hat{k}$  when the particle is moving from D to A
- (3)  $\vec{L} = -\frac{m\upsilon}{\sqrt{2}} R\hat{k}$  when the particle is moving from A to B
- (4)  $\vec{L} = m\upsilon \left[\frac{R}{\sqrt{2}} a\right]\hat{k}$  when the particle is moving from C to D.

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Sol.  $\vec{L} = -\frac{m_0}{\sqrt{2}} R\hat{k}$  when particle is moving from D to A.  $\vec{L} = m_0 \left[ \frac{R}{\sqrt{2}} + a \right] \hat{k}$  when the particle is moving from C to D.

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6. Choose the correct statement :

(1) In frequency modulation the amplitude of the high frequency carrier wave is made to vary in proportion to the amplitude of the audio signal

(2) In frequency modulation the amplitude of the high frequency carrier wave is made to vary in proportion to the frequency of the audio singal

(3) In amplitude modulation the amplitude of the high frequency carrier wave is made to very in proportion to the amplitude of the audio signal

(4) In amplitude modulation the frequency of the high frequency carrier wave is made to vary in proportion to the amplitude of the audio signal

- Sol. In amplitude modulation the amplitude of the high frequency carrier wave is made to very in proportion to the amplitude of the audio signal
- 7. Radiation of wavelength  $\lambda$ , is incident on a photocell. The fastest emitted electron has speed  $\upsilon$ . If the

wavelength is changed to  $\frac{3\lambda}{4}$ , the speed of the fastest emitted electron will be :

$$(1) = \upsilon \left(\frac{4}{3}\right)^{\frac{1}{2}} \qquad (2) = \upsilon \left(\frac{3}{4}\right)^{\frac{1}{2}} \qquad (3) > \upsilon \left(\frac{4}{3}\right)^{\frac{1}{2}} \qquad (4) < \upsilon \left(\frac{4}{3}\right)^{\frac{1}{2}}$$

Sol.  $\frac{hc}{\lambda} - \phi = \frac{1}{2}mv^2$ 

$$\frac{4hc}{3\lambda} - \phi = \frac{1}{2}m(v')^2 \quad (2)$$
  
Multiplying equation (1) by 4/3  
$$\frac{4}{3}\frac{hc}{\lambda} - \phi - \frac{\phi}{3} = \frac{1}{2}m\left(\frac{4}{3}v^2\right) \quad \dots \quad (3)$$
  
From (2) and (3)  
$$\frac{1}{2}m\left(\frac{4}{3}v^2\right) + \frac{\phi}{3} = \frac{1}{2}m(v')^2$$
  
Hence v' >  $v\left(\frac{4}{3}\right)^{\frac{1}{2}}$ 

(1)

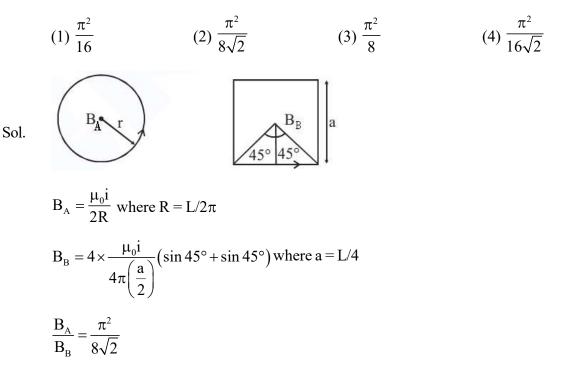
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8. Two identical wites A and B, each of length '*l*' carry the same current I. Wire A is bent into a circle of radius R and wire B is bent to form a square of side 'a'. If  $B_A$  and  $B_B$  are the values of magnetic field at the centres

of the circle and square respectively, then the ratio  $\frac{B_A}{B_B}$  is :

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9. A pipe open at both ends has a fundamental frequency f in air. The pipe is dipped vertically in water so that half of it is in water. The fundamental frequency of the air column is now :

(1) 2f (2) f (3) 
$$\frac{f}{2}$$
 (4)  $\frac{3f}{4}$ 

For the pipe open at both the ends,  $f_0 = \frac{v}{2L}$ 

For the pipe closed at one end and half length, 
$$f_0' = \frac{v}{4\left(\frac{L}{2}\right)}$$

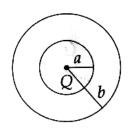
 $f_0' = f_0$ 

Sol.

10. The region between two concentric spheres of radii 'a' and 'b', respectively (see figure), has volume charge density  $\rho = \frac{A}{r}$ , where A is a constant and r is the distance from the centre. At the centre of the spheres is a point charge Q. The value of A such that the electric field in the region between the spheres will be constant



is:



(1) 
$$\frac{2Q}{\pi(a^2-b^2)}$$
 (2)  $\frac{2Q}{\pi a^2}$  (3)  $\frac{Q}{2\pi a^2}$  (4)  $\frac{Q}{2\pi(b^2-a^2)}$ 

Sol. Electric field in the region between the 2 spheres

 $E = \frac{K\left(Q + \int_{a}^{r} \frac{A}{r} \times 4\pi r^{2} dr\right)}{r^{2}}$  $= \frac{K\left[Q + 4\pi A\left(\frac{r^{2} - a^{2}}{2}\right)\right]}{r^{2}}$ 

For E to be independent of r,  $Q - \frac{4\pi Aa^2}{2} = 0$ 

$$A = \frac{Q}{2\pi a^2}$$

- 11. An arc lamp requires a direct current of 10 A at 80 V to function. If it is connected to a 220 V (rms), 50 Hz AC supply, the series inductor needed for it to work is close to :
- (1) 0.044 H (2) 0.065 H (3) 80 H (4) 0.08 H Sol.  $R = \frac{80}{10} = 8\Omega$  $i = 10 = \frac{220}{\sqrt{R^2 + (\omega L)^2}}$ where  $\omega = 2\pi \times 50$ L = 0.065 H
- 12. 'n' moles of an ideal gas undergoes a process  $A \rightarrow B$  as shown in the figure. The maximum temperature of the gas during the process will be

 $P_{0} \xrightarrow{P} A_{0} \xrightarrow{B} V_{0} \xrightarrow{V_{0}} V_{0} \xrightarrow{V_{0}} V_{0}$ 

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$(1) \frac{9P_0V_0}{2nR}$	$(2) \frac{9P_0V_0}{nR}$	$(3) \frac{9P_0V_0}{4nR}$	$(4) \frac{3P_0V_0}{2nR}$

Sol. For the given P–V graph,

$$P = -\left(\frac{P_0}{V_0}\right)V + 3P_0$$
$$T = \frac{PV}{nR} = \left(3P_0V - \frac{P_0}{V_0}V^2\right)\frac{1}{nR}$$

For maximum temperature,  $\frac{dT}{dV} = 0$ 

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$$T_{max} = \frac{9P_0V_0}{4nR}$$

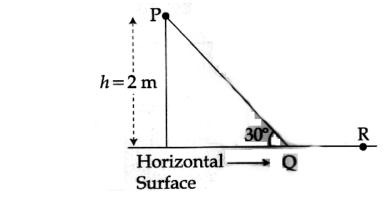
13. A person trying to lose weight by burning fat lifts a mass of 10 kg upto a height of 1 m 1000 times. Assume that the potential energy lost each time he lowers the mass is dissipated. How much fat will he use up considering the work done only when the weight is lifted up ? Fat supplies  $3.8 \times 10^7$  J of energy per kg which is converted to mechanical energy with a 20% efficiency rate. Take g = 9.8 ms<sup>-2</sup>:

(1)  $9.89 \times 10^{-3}$  kg (2)  $12.89 \times 10^{-3}$  kg (3)  $2.45 \times 10^{-3}$  kg (4)  $6.45 \times 10^{-3}$  kg

Sol. Work done =  $1000 \times mgh = 9.8 \times 10^4 J$ Let x kg of fat is used.

$$x \times 3.8 \times 10^7 \times \frac{20}{100} = 9.8 \times 10^4 \text{ J}$$
  
 $x = 12.89 \times 10^{-3} \text{ kg}$ 

14. A point particle of mass m, moves along the uniformly rough track PQR as shown in the figure. The coefficient of friction, between the particle and the rough track equals  $\mu$ . The particle is released, from rest, from the point P and it comes to rest at a point R. The energies, lost by the ball, over the parts, PQ and QR, of the track, are equal to each other, and no energy is lost when particle changes direction from PQ to QR. The values of the coefficient of friction  $\mu$  and the distance x(=QR), are, respectively close to:



(1) 0.29 and 3.5 m (2) 0.29 and 6.5 m (3) 0.2 and 6.5 m (4) 0.2 and 3.5 m

Sol. Total energy lost from P to  $R = mg \times 2$ 

$$\mu \left( \operatorname{mg} \cos 30^{\circ} \right) \left( \frac{2}{\sin 30^{\circ}} \right) = \frac{\operatorname{mg} \times 2}{2}$$

 $\mu$ mg × x =  $\frac{mg \times 2}{2}$  (where x is distance travelled from Q to R)

 $\mu = 0.29 \& x = 3.5m$ 

**15.** The temperature dependence of resistances of Cu and undoped Si in the temperature range 300-400 K, is best described by :

- (1) Linear increase for Cu, exponential decrease for Si
- (2) Linear decrease for Cu, linear decrease for Si
- (3) Linear increase for Cu, linear increase for Si
- (4) Linear increase for Cu, exponential increase for Si
- Sol. For metals,

 $\mathbf{R} = \mathbf{R}_0 \left( 1 + \alpha \Delta \mathbf{T} \right)$ 

Hence, for copper resistance increases linearly.

For silicon, since it is a semiconductor its resistance decreases exponentially

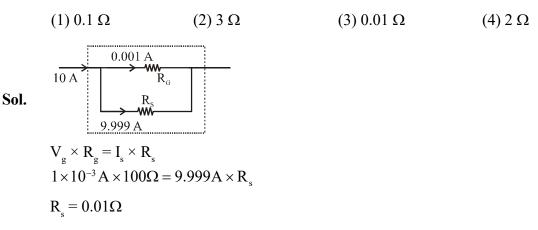
16. Arrange the following electromagnetic radiations per quantum in the order of increasing energy :

A:Blue light	B: Yelloe light	C : X-ray	D:Radiowave
(1) C, A, B, D	(2) B, A, D, C	(3) D, B, A, C	(4) A, B, D, C

Sol. As  $\lambda$  decreases energy increases.

Increases order of energy will be radiowave < yellow light <br/> blue light < X-ray

17. A galvanometer having a coil resistance of  $100 \Omega$  gives a full scale deflection, when a current of 1 mA is passed through it. The value of the resistance, which can convert this galvanometer into ammeter giving a full scale deflection for a current of 10 A, is :



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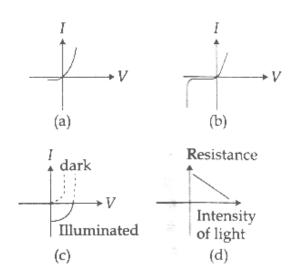
- 18. Half-lives of two radioactive elements A and B are 20 minutes and 40 minutes, respectively. Initially, the samples have equal number of nuclei. After 80 minutes the ratio of decayed numbers of A and B nuclei will be
  - (1) 1:4 (2) 5:4 (3) 1:16 (4) 4:1
- Sol. Number of half lives of A in 80 minutes = 4 Number of half lives of B in 80 minutes = 2

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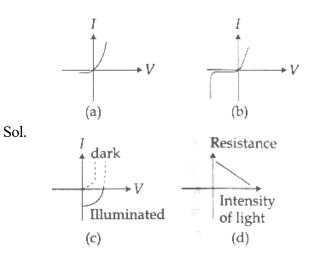
$$\frac{\text{decayed nuclei of A}}{\text{decayed nuclei of B}} = \frac{N - \frac{N}{16}}{N - \frac{N}{4}} = \frac{5}{4}$$

19. Identify the semiconductor devices whose characteristics are given below, in the order (a), (b), (c), (d) :

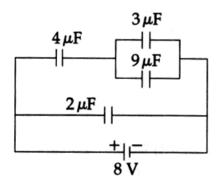


Solar cell, Light dependent resistance, Zener diole, Simple diode
 Zener diode, Solar cell, Simple diode, Light dependent resistance
 Simple diode, Zener diode, Solar cell, Light dependent resistance

(4) Zener diode, Simple diode, Light dependent resistance, Solar cell



- (a)  $\rightarrow$  Simple diode
- $(b) \rightarrow Zener diode$
- $(c) \rightarrow Solar cell$
- $(d) \rightarrow Light dependent resistance$
- 20. A combination of capacitors is set up as shown in the figure. The magnitude of the electric field, dur to a point charge Q (having a charge equal to the sum of the chargs on the 4  $\mu$ F and 9  $\mu$ F capacitors), at a point distant 30 m from it, would equal :



- (1) 420 N/C (2) 480 N/C (3) 240 N/C (4) 360 N/C
- Sol. Charge on  $4\mu$ F capacitor =  $24 \mu$ C Charge on  $9\mu$ F capacitor =  $18 \mu$ C So total charge Q =  $24 + 18 = 42 \mu$ C

$$E = \frac{KQ}{r^2}, r = 30 m$$
$$= 420 N/C$$

Sol.

21. A satellite is revolving in a circular orbit at a height 'h' from the earth's surface (radius of earth R;  $h \le R$ ). The minimum increase in its orbital velocity required, so that the satellite could escape from the earth's gravitational field, is close to : (Neglect the effect of atmosphere)

(1) 
$$\sqrt{gR/2}$$
 (2)  $\sqrt{gR} \left(\sqrt{2} - 1\right)$  (3)  $\sqrt{2gR}$  (4)  $\sqrt{gR}$   
 $\frac{GMm}{R^2} = \frac{mv^2}{R}$   
 $v = \sqrt{\frac{GM}{R}} = \sqrt{gR}$   
 $v_{escape} = \sqrt{2gR}$   
 $\Delta v = \sqrt{gR} \left(\sqrt{2} - 1\right)$ 

22. A screw gauge with a pitch of 0.5 mm and a circular scale with 50 divisions is used to measure the thickness of a thin sheet of Aluminium. Before starting the measurement, it is found that when the two jaws of the screw gauge are brought in contact, the 45<sup>th</sup> division coincides with the main scale line and that the zero of

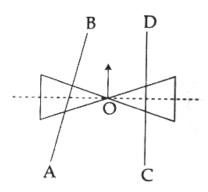
the main scale is barely visible. What is the thickness of the sheet if the main scale reading is 0.5 mm and the  $25^{\text{th}}$  division coincides with the main scale line ?

(1) 0.70 mm (2) 0.50 mm (3) 0.75 mm (4) 0.80 mm Sol. Least count =  $\frac{0.5}{50}$  mm = 0.01mm It has negative error = 5 × 0.01 = 0.05 mm Reading = (0.5 + 25 × 0.01) + 0.05  $\Rightarrow 0.80$  mm

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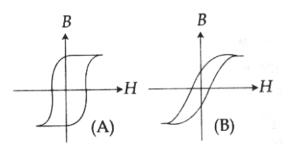
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23. A roller is made by joining together two cones at their vertices O. It is kept on two rails AB and CD which are placed asymmetrically (see figure), with its axis perpendicular to CD and its centre O at the centre of line joining AB and CD (see figure). It is given a light push so that it starts rolling with its centre O moving paralel to CD in the direction shwon. As it moves the roller will tend to :



(1) go straight (2) turn left and right alternately (3) turn left (4) turn right

- Sol. The roller will trun left.
- 24. Hysteresis loops for two magnetic materials A and B are given below :



These materials are used to make magnets for electric generators, transformer core and electromagnet core. Then it is proper to use :

- (1) A for transformers and B for electric generators (2) B for electromagnets and transformers
- (3) A for electric generators and transformers (4) A for electromagnets and B for electric generators
- Sol. For electromagnets and transformers, core should be quickly magnetized and demagnetized, therefore B should be used.

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25. The box of a pin hole camera, of length L, has a hole of radius a. It is assumed that when the hole is illuminated by a parallel beam of light of wavelength  $\lambda$  the spread of the spot (obtained on the opposite wall of the camera) is the sum of its geometrical spread and the spread due to diffraction. The spot would then have its minimum size (say  $b_{min}$ ) when :

(1) 
$$a = \sqrt{\lambda L}$$
 and  $b_{\min} = \sqrt{4\lambda L}$   
(2)  $a = \frac{\lambda^2}{L}$  and  $b_{\min} = \sqrt{4\lambda L}$   
(3)  $a = \frac{\lambda^2}{L}$  and  $b_{\min} = \left(\frac{2\lambda^2}{L}\right)$   
(4)  $a = \sqrt{\lambda L}$  and  $b_{\min} = \left(\frac{2\lambda^2}{L}\right)$ 

Spot size (diameter)  $b = 2\left(\frac{\lambda L}{2a}\right) + 2a$ 

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$$\label{eq:a2} \begin{split} &a^2 + \lambda L - ab = 0 \\ & \text{For Real roots } b^2 - 4L\lambda \geq 0 \end{split}$$

Sol.

$$b_{min.} = \sqrt{4\lambda L}$$
  
 $a = \sqrt{\lambda L}$ 

26. A uniform string of length 20 m is suspended from a rigid support. A short wave pulse is introduced at its lowest end. It starts moving up the string. The time taken to reach the support is :

(3)  $2\pi\sqrt{2}$  s

l] dx

(4) 2 s

(Take g = 10 ms<sup>-2</sup>) (1)  $2\sqrt{2}$  s

Tension at a distance x from lower end,

(2)  $\sqrt{2}$  s

 $T=(\mu x) g \{\mu \text{ is mass per unit length}\}$ 

$$v = \sqrt{\frac{T}{\mu}} = \sqrt{xg}$$
$$\frac{dx}{dt} = \sqrt{xg}$$
$$\int_{0}^{20} \frac{dx}{\sqrt{x}} = \sqrt{g} \int_{0}^{t} dt$$
$$t = 2\sqrt{2}$$

27. An ideal gas undergoes a quasi static, revesible process in which its molar heat capacity C remains constant. If during this process the relation of pressure P and volume V is given by  $PV^n = constant$ , then n is given by (Here  $C_p$  and  $C_v$  are molar specific heat at constant pressure and constant volume, respectively) :

(1) 
$$n = \frac{C_p - C}{C - C_v}$$
 (2)  $n = \frac{C - C_v}{C - C_p}$  (3)  $n = \frac{C_p}{C_v}$  (4)  $n = \frac{C - C_p}{C - C_v}$ 



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Sol. 
$$C = C_v - \frac{R}{n-1}$$

Find n & substitute  $R = C_p - C_v$ 

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- 28. An observer looks at a distant tree of height 10 m with a telescope of magnifying power of 20. To the observer the tree appears :
  - (1) 20 times taller (3) 10 times taller (2) 20 times nearer (4) 10 times nearer  $=\frac{h_{I}/x}{h_{o}/x}$

Sol. 
$$m = \frac{\theta'}{\theta} =$$

Sol.

$$20 = \frac{h_{I}}{10}$$

29. In an experiment for determination of refractive index of glass of a prism by  $i - \delta$ , plot, it was found that a ray incident at angle 35°, suffers a deviation of 40° and that it emerges at angle 79°. In that case which of the following is closest to the maximum possible value of the refractive indes?

(1) 1.7  
(2) 1.8  
(3) 1.5  
(4) 1.6  

$$\mu = \frac{\sin\left(\frac{A+\delta_{\min}}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$
(1)  

$$\delta = 40 = i + e - A$$

$$A = 74^{\circ}$$
If we put  $\delta_{\min} = 40^{\circ}$  (actually  $\delta_{\min}$  will definitely be less than  $40^{\circ}$ ) &  $A = 74^{\circ}$  then  $\mu \approx 1.4$   
 $\therefore \delta_{\min} < 40^{\circ}$   
 $\therefore \mu < 1.4$ 

**30.** A pendulum clock loses 12 s a day if the temperature is  $40^{\circ}$ C and gains 4 s a day if the temperature is

20°C. The temperature at which the clock will show correct time, and the co-efficient of linear expansion

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 $\left(\alpha\right)$  of the metal of the pendulum shaft are respectively :

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 $\alpha = 1.85 \times 10^{-5/\circ}C$ 

Sol.

(1)  $30^{\circ}C; \alpha = 1.85 \times 10^{-3/\circ}C$ (2)  $55^{\circ}C; \alpha = 1.85 \times 10^{-2/\circ}C$ (3)  $25^{\circ}C; \alpha = 1.85 \times 10^{-5/\circ}C$ (4)  $60^{\circ}C; \alpha = 1.85 \times 10^{-4/\circ}C$   $T = 2\pi\sqrt{\frac{L}{g}}$   $\frac{\Delta T}{T} = \frac{1}{2}\frac{\Delta L}{L} = \frac{1}{2}\alpha\Delta\theta$   $\Delta T = T \times \frac{1}{2}\alpha\Delta\theta$   $12 = T \times \frac{1}{2}\alpha(40 - T)$  (1)  $4 = T \times \frac{1}{2}\alpha(T - 20)$  (2) Divide (1) by (2)  $T = 25^{\circ}C$