JEE Main July 2021 Question Paper With Text Solution 27 July. | Shift-1

PHYSICS



JEE Main & Advanced | XI-XII Foundation| VI-X Pre-Foundation



JEE MAIN JULY 2021 | 27th JULY SHIFT-1

SECTION – A

1. The number of molecules in one litre of an ideal gas at 300 K and 2 atmospheric pressure with means kinetic energy 2×10^{-9} J per molecule is :

(1) 1.5×10^{11} (2) 6×10^{11} (3) 0.75×10^{11} (4) 3×10^{11}

Ans. Official Answer NTA (1)

Sol.
$$PV = nRT$$

$$PV = \frac{N}{NA}RT - (1)$$
$$KE = \frac{3}{2}KT - (2)$$

From (1) & (2) N =
$$\frac{PV}{\frac{2}{3}(KE)} = \frac{2 \times 10^{-3} \times 10^{3}}{\frac{2}{3} \times 2 \times 10^{-9}} = 1.5 \times 11$$

2. Two identical tennis balls each having mass 'm' and charge 'q' are suspended from a fixed point by threads of length '*l*'. What is the equilibrium separation when each thread makes small amgle 'θ' with the vertical ?

11

(1)
$$\mathbf{x} = \left(\frac{q^2 l^2}{2\pi\epsilon_0 m^2 g}\right)^{\frac{1}{3}}$$

(2) $\mathbf{x} = \left(\frac{q^2 l^2}{2\pi\epsilon_0 m^2 g^2}\right)^{\frac{1}{3}}$
(3) $\mathbf{x} = \left(\frac{q^2 l}{2\pi\epsilon_0 m g}\right)^{\frac{1}{2}}$
(4) $\mathbf{x} = \left(\frac{q^2 l}{2\pi\epsilon_0 m g}\right)^{\frac{1}{3}}$

Ans. Official Answer NTA (4)

Sol.

$$F_{E} \xleftarrow{} d/2 \rightarrow \xleftarrow{$$

 $T\cos\theta = mg - (2)$



 $\frac{2}{1}$ \Rightarrow tan $\theta = \frac{F_E}{mg}$

 θ is small so $\tan \theta \approx \sin \theta$

$$\sin \theta = \frac{Kq^2}{d^2} = \frac{d/2}{l}$$
$$\frac{Kq^2}{d^2mg} = \frac{d}{2l}$$
$$d = \left[\frac{2Kq^2l}{mg}\right]^{1/3}$$
$$d = \left(\frac{q^2l}{2\pi\varepsilon_a mg}\right)^{1/3}$$

3. Assertion A : If in five complete rotaions of the circular scale, the distance travelled on main scale of the screw gauge is 5 mm and there are 50 total divisions on circular scale, then least count is 0.001 cm.

Reason R : Least Count = $\frac{\text{Pitch}}{\text{Total divisions on circular scale}}$

In the light of the above statements, choose the most appropriate answer from the options given below :

(1) A is not correct but R is correct.

(2) A is correct but R is not correct.

(3) Both A and R correct and R is the correct explanation of A.

(4) both A and R are correct and R is NOT the correct explanation of A.

Ans. Official Answer NTA (1)

Sol. In 5 revolution distance travel 5mm

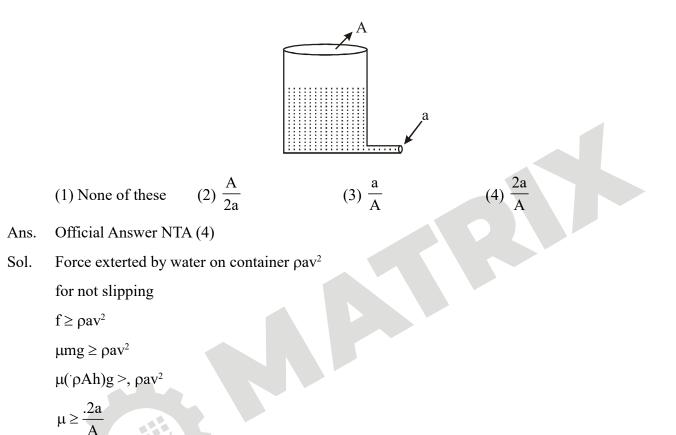
In 1 revolution distance travel 1mm

so least count =
$$\frac{1}{50} = 0.02$$

reason is also correct but it is not explanation of A

4. A light cylindrical vessel is kept on a horizontal surface. Area of base is A. A hole of cross-sectional area 'a' is made just at its bottom side. the minimum coefficient of friction necessary to prevent sliding the vessel due to the impact force of the emerging liquid is (a << A):

MATRIX



5. Three objects A, b and C are kept in a straight line on frictionless horizontal surface. the masses of A, B and C are m, 2 m and 2 m respectively. A moves towards B with a speed of 9m/s and makes an elastic collision with it. Thereafter B makes a completely inelastic collision with C. all motions occur along same straight line. The final speed of C is :

A B C
m 2 m 2 m
(1) 4 m/s (2) 3 m/s (3) 9 m/s (4) 6 m/s
Ans. Official Answer NTA (2)
Sol. Collision b/w A & B

$$V_1 \leftarrow A$$
 $B \rightarrow V_2$
 $m(9) + O = -mV_1 + 2mV_2$



$$9 = -V_1 + 2V_2 - (1)$$

$$1 = \frac{V_2 + V_1}{9 - 0}$$

$$V_2 + V_1 = 9 - (2)$$
from (1) & (2) $\Rightarrow V_1 = 3 V_2 =$
Collision between B & C
$$\boxed{B + C} \longrightarrow V_0$$
(2m) (6) = 4mV_0
$$V_0 = 3 m/s$$

6. A particle starts executing simple harmonic motion (SHM) of amplitude 'a' and total energy E. At any

instant, its kinetic energy is $\frac{3E}{4}$ then its displacement 'y' is given by :

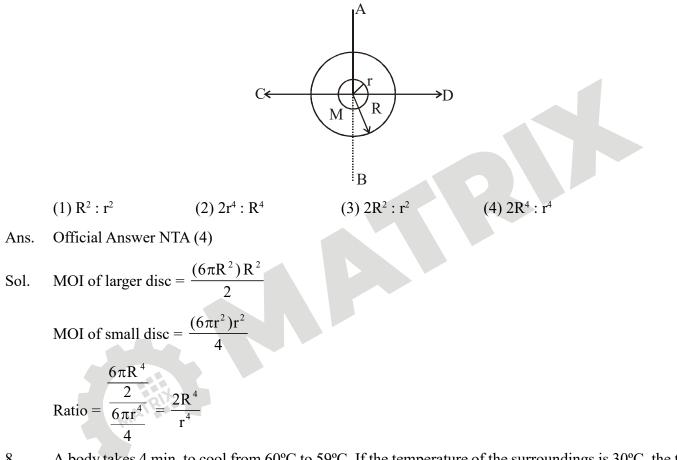
6

(1)
$$y = \frac{a}{\sqrt{2}}$$
 (2) $y = \frac{a\sqrt{3}}{2}$ (3) $y = a$ (4) $y = \frac{a}{2}$

Ans. Official Answer NTA (4)

Sol.
$$KE = \frac{K}{2} \left[a^2 - y^2 \right]$$
$$E = \frac{K}{2} a^2$$
$$\frac{3K}{4} = \frac{K}{2} (a^2 - y^2)$$
$$\frac{3}{4} \left(\frac{K}{2} a^2 \right) = \frac{K}{2} (a^2 - y^2)$$
$$y = \pm a/2$$

7. The figure shows two solid discs with radius R and r respectively. If mass per unit area is same for both, what is the ratio of MI of bigger disc around axis AB (which is ⊥ to the plane of the disc and passing through its centre) to MI of smaller disc around one of its diameters lying on its plane ? Given 'M' is the mass of the larger disc. (MI stands for moment of inertia)



- A body takes 4 min. to cool from 60°C to 59°C. If the temperature of the surroundings is 30°C, the time taken by the body to cool from 51°C to 49°C is :
 - (1) 8 min. (2) 6 min. (3) 3 m

(3) 3 min.

(4) 4 min.

Ans. Official Answer NTA (4)

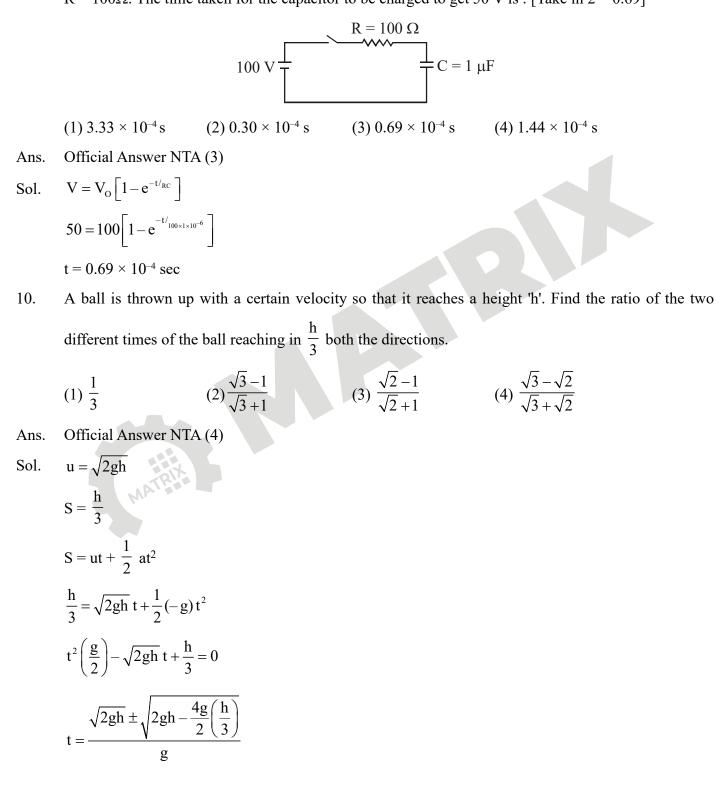
MATRIX

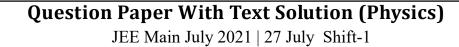
Sol.
$$\frac{\Delta T}{\Delta t} = K[T_{av} - T_s]$$
$$\frac{61 - 59}{4} = K\left[\frac{61 + 59}{2} - 30\right] - (1)$$
$$\frac{51 - 49}{t} = K\left[\frac{51 + 49}{2} - 30\right] - (2)$$

From (1) & (2) t = 6 min.

9. A capacitor of capacitance $C = 1 \ \mu F$ is suddenly connected to a battery of 100 volt through a resistance $R = 100\Omega$. The time taken for the capacitor to be charged to get 50 V is : [Take ln 2 = 0.69]

MATRIX





$$\frac{t_1}{t_2} = \frac{\sqrt{2gh} - \sqrt{\frac{4gh}{3}}}{\sqrt{2gh} + \sqrt{\frac{4gh}{3}}} = \frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} + \sqrt{2}}$$

MATRIX

11. In young's double slit experiment, if the source of light changes from orange to blue then :

- (1) The distance between consecutive fringes will decrease.
- (2) The central bright fringe will become a dark fringe.
- (3) the distance between consecutive fringes will increase.
- (4) The intensity of the mina will increase.
- Ans. Official Answer NTA (1)

Sol. Fringe width = $\frac{\lambda D}{d}$

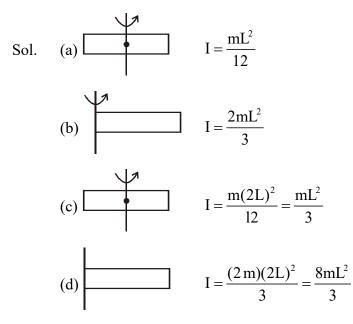
 $\lambda \downarrow$ fringe width \downarrow

12. List - I List - II (a) MI of the rod (length L, Mass M, about an axis (i) 8 ML²/3 \perp to the rod passing through the midpoint) (b) MI of the rod (length L, Mass 2m, about an axis (ii) $Ml^2/3$ \perp to the rod passing through one of its end) (c) MI of the rod (length 2L, Mass M, about an axis (iii) ML²/12 \perp to the rod passing through its midpoint) (d) MI of the rod (length 2L, Mass 2M, aboutan axis (iv) $2ML^{2}/3$ \perp to the rod passing through one of its end) Choose the correct answer from the options given below : (1) (a)–(ii), (b)–(i), (c)–(iii), (d)–(iv) (2) (a)–(iii), (b)–(iv), (c)–(i), (d)–(ii) (3) (a)-(ii), (b)-(iii), (c)-(i), (d)-(iv)

(4) (a)–(iii), (b)–(iv), (c)–(ii), (d)–(i)



Ans. Official Answer NTA (4)



13. Two capacitors of capacities 2C and C are joined in parallel and charged up to potential V. The battery is removed and the capacitor of capacity C is filled completely with a medium of dielectric constant K. The potential difference across the capacitors will now be :

(1)
$$\frac{V}{K}$$
 (2) $\frac{3V}{K}$ (3) $\frac{V}{K+2}$ (4) $\frac{3V}{K+2}$

Ans. Official Answer NTA (4)

CV(



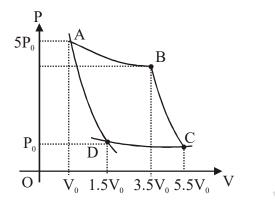
2C

From charge conservation

V

$$2CV + CV = (2C + KC)V_{nev}$$
$$\frac{3V}{2 + K} = V_{new}$$

14. In the reported figure, there is a cyclic proces ABCDA on a sample of 1 mol of a diatomic gas. The temperature of the gas during the process $A \rightarrow B$ and $C \rightarrow D$ are T_1 and T_2 ($T_1 > T_2$) respectively.



Choose the correct option out of the following for work done if processes BC and DA are adiabatic.

(1)
$$W_{AB} = W_{DC}$$
 (2) $W_{AD} = W_{BC}$ (3) $W_{AB} < W_{CD}$ (4) $W_{BC} + W_{DA} > 0$

Ans. Official Answer NTA (2)

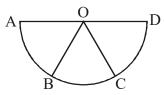
MATRIX

Sol. Work done = $\frac{-nR(T_f - T_1)}{\gamma - 1}$

$$W_{AD} = \frac{-nR}{\gamma - 1} (T_2 - T_1)$$
$$W_{BD} = \frac{-nR}{\gamma - 1} (T_2 - T_1)$$
$$W_{AD} = W_{BC}$$

15. Assertion A : If A, B, C, D are four points on a semi-circular arc with centre at 'O' such that $|\overrightarrow{AB}| = |\overrightarrow{BC}| = |\overrightarrow{CD}|$, then

 $\overrightarrow{AB} + \overrightarrow{AC} + \overrightarrow{AD} = 4\overrightarrow{AO} + \overrightarrow{OB} + \overrightarrow{OC}$ Reason R : Polygon law of vector addition yields $\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CD} = \overrightarrow{AD} = 2\overrightarrow{AO}$



In the light of the above statements, choose the most appropriate answer from the options given below :

(1) A is correct but R is not correct.

- (2) Both A and R are correct but R is not the correct explanation of A.
- (3) Both A and R are correct and R is the correct explanation of A.
- (4) A is not correct but R is correct.
- Ans. Official Answer NTA (2)

MATRIX

Sol. $\overrightarrow{OA} + \overrightarrow{AB} = \overrightarrow{OB} - (1)$ $\overrightarrow{OB} + \overrightarrow{BC} = \overrightarrow{OC} - (2)$ $\overrightarrow{OC} + \overrightarrow{CD} = \overrightarrow{OD} - (3)$ $\overrightarrow{AB} + \overrightarrow{CB} = \overrightarrow{OA}$ $\overrightarrow{AC} = \overrightarrow{OC} - \overrightarrow{OA}$ $\overrightarrow{AD} = \overrightarrow{OD} - \overrightarrow{OA}$ $= \overrightarrow{OA} - \overrightarrow{OA}$ SO $\overrightarrow{AB} + \overrightarrow{AC} + \overrightarrow{AD} = \overrightarrow{OB} + \overrightarrow{OC} - 4\overrightarrow{OA}$ $= 4\overrightarrow{AO} + \overrightarrow{OB} + \overrightarrow{OC}$ for reason $\rightarrow \overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CD} + \overrightarrow{DA} = O$ $\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CD} = \overrightarrow{AD} = 2\overrightarrow{AO}$

both statement are correct but is not correct explanation of A.

]

16. A 0.07 H inductior and a 12Ω resistor are connected in series to a 220 V, 50 hz ac source. The approximate current in the circuit and the phase angle between current and source voltage are

respectively. [Take
$$\pi$$
 as $\frac{22}{7}$
(1) 8.8 A and $\tan^{-1}\left(\frac{6}{11}\right)$
(2) 88 A and $\tan^{-1}\left(\frac{11}{6}\right)$
(3) 8.8 A and $\tan^{-1}\left(\frac{11}{6}\right)$
(4) 0.88 A and $\tan^{-1}\left(\frac{11}{6}\right)$

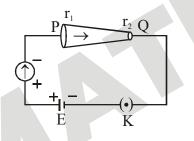
Ans. Official Answer NTA (3)



Sol.
$$\phi = \tan^{-1}\left(\frac{X_L}{R}\right)$$

 $\phi = \tan^{-1}\left(\frac{0.07 \times 2\pi(50)}{12}\right)$
 $\phi = \tan^{-1}\left(\frac{11}{6}\right)$
 $Z = \sqrt{X_L^2 + R^2} = 25.059$
 $I = \frac{V}{Z} = \frac{220}{\sqrt{X_L^2 + R^2}} = 8.8A$

17. In the given figure, a battery of emf E is connected across a conductor PQ of length 'l' and different of cross-sections having radii r_1 and r_2 ($r_2 < r_1$).



Choose the correct option as one moves from P to Q :

- (1) All of these
- (2) Electron current decreases
- (3) Electric field decreases.
- (4) Drift velocity of electron increases.
- Ans. Official Answer NTA (4)
- Sol. Current is constant

$$i = neAvd \Longrightarrow Vd \propto \frac{1}{A}$$
$$J = \sigma E \cdot J = \frac{1}{A} \Longrightarrow E \propto \frac{1}{A}$$
$$A \downarrow E \uparrow Vd \uparrow$$

18. If 'f denotes the ratio of the number of nuclei decayed (N_d) to the number of nuclei at t = 0 (N_0) then for a collection of radioactive nuclei, the rate of change of 'f with respect to time is given as :

 $[\lambda \text{ is is the radioactive decay constant}]$

(1) $\lambda(1 - e^{-\lambda t})$ (2) $-\lambda e^{-\lambda t}$ (3) $\lambda e^{-\lambda t}$ (4) $-\lambda(1 - e^{-\lambda t})$ Official Answer NTA (3)

Sol.
$$N = N_0 e^{-\lambda t}$$

Ans.

$$N_{d} = N_{o} - N$$

$$N_{o} - N_{d} = N_{o}e^{-\lambda t}$$

$$N_{d} = N_{o}(1 - e^{-\lambda t})$$

$$\frac{N_{d}}{N_{o}} = f = 1 - \lambda e^{-\lambda t}$$

$$\frac{dt}{dt} = \lambda e^{-\lambda t}$$

MATRIX

19. The relative permittivity of distilled water is 81. The velocity of light in it will be : (Given $\mu_r = 1$) (1) 3.33×10^7 m/s (2) 4.33×10^7 m/s (3) 2.33×10^7 m/s (4) 5.33×10^7 m/s Ans. Official Answer NTA (1)

Sol.
$$V = \frac{C}{\sqrt{\mu_r \varepsilon_r}} = \frac{3 \times 10^8}{\sqrt{(81)(1)}} = \frac{3 \times 10^8}{9}$$

= 3.33 × 10⁷

20. In the reported figure, a capacitor is formed by placing a compound dielectric between the plates of parallel plate capacitor. The expression for the capacity of the said capacitor will

$$(1) \frac{15}{34} \frac{K\varepsilon_0 A}{d} \qquad (2) \frac{9}{6} \frac{K\varepsilon_0 A}{d} \qquad (3) \frac{25}{6} \frac{K\varepsilon_0 A}{d} \qquad (4) \frac{15}{6} \frac{K\varepsilon_0 A}{d}$$



Ans. Official Answer NTA (1)

Sol.
$$\frac{1}{\text{Ceq}} = \frac{d}{\text{K}\varepsilon_0 A} + \frac{2d}{3\text{K}\varepsilon_0 A} + \frac{3d}{5\text{K}\varepsilon_0 A}$$

 $Ceq = \frac{15K\varepsilon_0 A}{34d}$

SECTION - B

- 1. In Bohr's atomic model, the electron is assumed to revolve in a circular orbit of radius 0.5 Å. If the speed of electron is 2.2×10^6 m/s, then the current associated with the electron will $\times 10^{-2}$
 - mA. [Take π as $\frac{22}{7}$]

Ans. Official Answer NTA (112)

Sol.
$$I = \frac{q}{T} = \frac{q}{2\pi / \omega} = \frac{e\omega}{2\pi} = \frac{ev}{2\pi r}$$

= $\frac{(1.6 \times 10^{-19})(2.2 \times 10^6)}{2\pi (0.5 \times 10^{-10})} = 1.12 \text{ mA}$
 $I = 112 \times 10^{-2} \text{ mA}$

- 2. A transistor is connected in common emitter circuit configuration, the collector supple voltage is 10 V and the voltage drop across a resistor of 1000 Ω in the collector circuit is 0.6 V. If the current gain factor (β) is 24, then the base current is _____µA. (Round off to the Nearest Integer)
- Ans. Official Answer NTA 25

Sol. Rc = 1000
$$\Delta V = 0.6$$

Ic = $\frac{0.6}{1000} \Rightarrow$ Ic = 6×10^{-4}
B = $\frac{Ic}{I_B} \Rightarrow$ IB = $\frac{Ic}{B} = \frac{6 \times 10^{-4}}{24} = 25 \mu A$

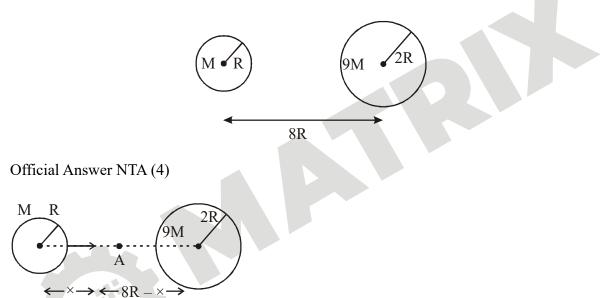
3. Suppose two planets (spherical in shape) of radii R and 2 R, but mass M and 9M respectively have a centre to centre separation 8 R as shown in the figure. A satellite of mass 'm' is projected from the surface of the planet of mass 'M' directly towards the centre of the second planet. the minimum speed 'v' required for the satellite to reach the surface of the second planet is $\sqrt{\frac{a}{7} \frac{GM}{R}}$ then the value of 'a' is

[Given : The two planets are fixed in their postion]

MATRIX

Ans.

Sol.



at point A acceleration due to gravity is zero so after point A satellite will attract by the planet 9m.

$$\frac{GM}{x^2} = \frac{G(9M)}{(8R-X)^2}$$

$$X = 2R$$
Velocity at point A is zero.
from conservation of energy
$$\frac{1}{2}mv^2 = \frac{GMm}{R} - \frac{G(9M/m)}{7R} = O - \frac{GMm}{2R} - \frac{G(9M)m}{6R}$$

$$V = \sqrt{\frac{4GM}{7R}}$$

- 4. A radioactive sample has an average life of 30 ms and is decaying. A capacitor of capacitance 200 μ F is first charged and later connected with resistor 'R'. If the ratio of charge on capacitor to the activity of radioactive sample is fixed with respect to time then the value of 'R' should be ______Ω.
- Ans. Official Answer NTA(150)

MATRIX

Sol.
$$Q = Q_0 e^{-t/RC} \qquad N = N_0 e^{-\lambda t}$$
$$\frac{Q}{N} = \frac{Q_0 e^{-t/RC}}{N_0 e^{-\lambda t}} = \frac{Q_0}{N_0} e^{t\left(1 - \frac{1}{RC}\right)}$$
$$\frac{Q}{N} \text{ is constant so } \lambda - \frac{1}{RC} = 0 \Longrightarrow \lambda = \frac{1}{RC}$$
$$R = \frac{1}{\lambda C} = \frac{Tm}{C} = \frac{30 \times 10^{-3}}{200 \times 10^{-6}} = 150$$

- 5. A particle of mass 9.1×10^{-31} kg travels in a medium with a speed of 10^6 m/s and a photon of a radiation of linear momentum 10^{-27} kg m/s in vacuum. The wavelength of photon is ______ times the wavelength of the particle.
- Ans. Official Answer NTA (910)

Sol. for photn
$$\lambda = \frac{h}{p} = \frac{6.6 \times 10^{-34}}{10^{-27}}$$

$$\lambda_2 = \frac{h}{mV} = \frac{6.6 \times 10^{-34}}{(9.1 \times 10^{-31})(10^6)}$$
$$\frac{\lambda_1}{\lambda_2} = 910$$

- 6. In a uniform magnetic field, the magnetic needle has a magnetic moment 9.85×10^{-2} A/m² and moment of inertia 5×10^{-6} kg m². If it performs 10 complete oscillations in 5 seconds then the magnitude of the magnetic field is _____mT. [Take π^2 as 9.86]
- Ans. Official Answer NTA (8)

Sol.
$$T = 2\pi \sqrt{\frac{I}{mB}}$$

 $T = \frac{1}{2}$

$$\frac{1}{2} = 2\pi \sqrt{\frac{5 \times 10^{-6}}{9.85 \times 10^{-2} (B)}}$$

MATRIX

 $B = 80 \times 10^{-4} = 8mT$

7. A stone of mass 20 g is projected from a rubber catapult of length 0.1 m and are of cross section 10^{-6} m² stretched by an amount 0.04 m. the velocity of the projected stone is _____ m/s. (Young's modulus of rubber = 0.5×10^9 N/m²)

Ans. Official Answer NTA (20)

Sol. From energy conservation

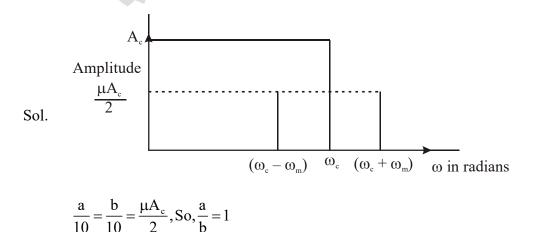
$$\frac{1}{2} \left(\frac{YA}{L} \right) x^2 = \frac{1}{2} mV^2$$
$$v^2 = \left(\frac{0.5 \times 10^9 \times 10^{-6}}{0.1} \right) (0.04)^2$$

v = 20 m/s

8. The amplitude of upper and lower side bands of A.M. wave where a carrier signal with frequency 11.21 MHz, peak voltage 15V is amplitude modulated by a 7.7 kHz sine wave of 5V amplitude are $\frac{a}{10}$ V and

$$\frac{b}{10}$$
 V respectively. The the value of $\frac{a}{b}$ is _____

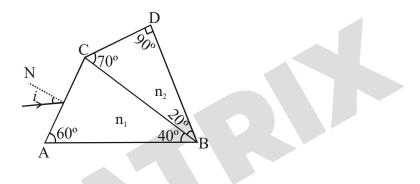
Ans. Official Answer NTA (1)



9. A prism of refractive index n_1 and another prism of refractive index n_2 are stuck together (as shown in the figure). n_1 and n_2 depend on λ , the wavelength of light, according to the relation

$$n_1 = 1.2 + \frac{10.8 \times 10^{-14}}{\lambda^2}$$
 and $n_2 = 1.45 + \frac{1.8 \times 10^{-14}}{\lambda^2}$

The wavelength for which rays incident at any angle on the interface BC pass through without bending at that interface will be _____nm.



Ans. Official Answer NTA (600)

MATRIX

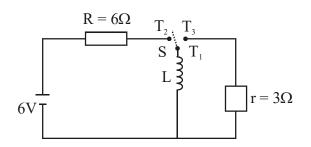
Sol. for no bending at surface BC

$$\mathbf{n}_1 = \mathbf{n}_2$$

$$1.2 + \frac{10.8 \times 10^{14} \times 10^{-6}}{\lambda^2} 1.45 + \frac{1.8 \times 10^{-4}}{\lambda^2}$$

$$\lambda = 600 \text{ nm}$$

10. Consider an electrical circuit containing a two way switch 'S'. Initially S is open and then T_1 is connected to T_2 . As the current in $R = 6\Omega$ attains a maximum value of steady state level, T_1 is disconnected from T_2 and immediately connected to T_3 . Potential drop across $r = 3 \Omega$ resistor immediately after T_1 is connected to T_3 is ______V. (Round off to the Nearest Interger)





Ans. Official Answer NTA (3)

MATRIX

Sol. When $T_1 \& T_2$ are connected, then, the steady state current in the inductor

$$I = \frac{6}{6} = lA$$

When $T_1 \& T_3$ are connected then current through inductor remains same. so potential difference across 3R V = Ir = 1 × 3 = 3Volt