JEE Main September 2020

Question Paper With Text Solution

2 September| Shift-1

PHYSICS

MATRIX

JEE Main & Advanced | XI-XII Foundation| VI-X Pre-Foundation

Office : Piprali Road, Sikar (Raj.) | Ph. 01572-241911

Website : www.matrixedu.in ; Email : smd@matrixacademy.co.in

JEE MAIN SEP 2020 | 2 SEP SHIFT-1

1. Interference fringes are observed on a screen by illuminating two thin slits 1 mm apart with a light source by illuminating two thin slits 1 mm apart with a light source (λ = 632.8 nm). The distance between the screen an the slits is 100 cm. If a bright fringe is observed on a screen at a distance of 1.27 mm from the central bright fringe, then the path difference between the waves, which are reaching this point from the slits is close to :

(A) $2.05\,\mu m$ (B) $2.87\,nm$ (C) $1.27\,\mu m$ (D) $2\,nm$

Ans. (C)

Sol. $\Delta P = d\sin\theta$

$= d\theta$

$$= \frac{dy}{D} = \frac{10^{-3} \times 1.270mm}{1m} = 1.270\mu m$$

2. Magnetic materials used for making permanent magnets (P) and magnets in a transformer (T) have different properties of the following, which property best matches for the type of magnet required?

(A) P : Small retentivity, large coercivity (B) T : Large retentivity, small coercivity

(C) P : Large retntivity, large coercivity (D) T : Large retentivity, large coercivity

Ans. (D)

Sol. Permanent magnets (P) required . large rectentivity and large coercivity.

3. Two identical strings X and Z made of same material have tension T_x and T_z in them. If their fundamental frequencies are 450 Hz and 300 Hz, respectively, then the ratio T_x/T_z is :

(A) 1.5 (B) 2.25 (C) 0.44 (D) 1.25

Ans. (B)

Sol. $$f_x = \frac{1}{2\ell}\sqrt{\frac{T_x}{\mu}}$$

$$f_z = \frac{1}{2\ell}\sqrt{\frac{T_z}{\mu}}$$

$$\frac{f_x}{f_z} = \frac{450}{300} = \sqrt{\frac{T_x}{T_z}}$$

$\Rightarrow T_x / T_z = 9/4$

4. If speed V, area A and force F are chosen as fundamental units, then the dimension of Young's modulus will be :

(A) FA^2V^{-2} (B) FA^2V^{-3} (C) $FA^{-1}V^0$ (D) FA^2V^{-1}

Ans. (C)

Sol. $Y \propto F^a V^b A^c$ $\quad Y = \left(\frac{F}{A}\right)$

$$\frac{MLT^{-2}}{L^2} \propto \left(M^1L^1T^{-2}\right)^a \left(L^1T^{-1}\right)^b \left(L^2\right)^c$$

$M^1L^{-1}T^{-2} \propto M^a L^{a+b+2c} T^{-2a-b}$

from dim of M $\Rightarrow$ a = 1 ....(1)

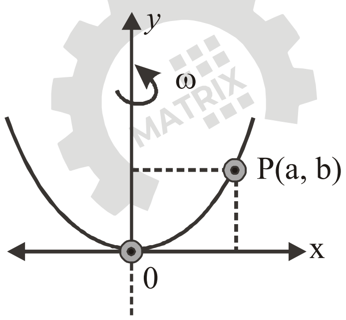
from dim of L $\Rightarrow$ a + b + 2c = –1 ....(2)

from dim of T $\Rightarrow$ –2a + b = –2 ....(3)

from (1), (2) and (3) a = 1, b = 0, c = –1

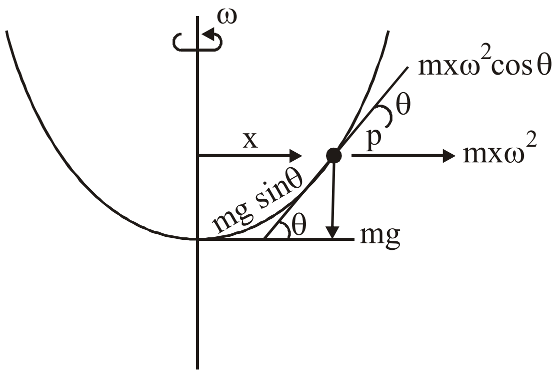
$Y = F^1 v^0 A^{-1}$

5. A bead of mass m stays at point P(a, b) on a wire bent in the shape of a parabola $y = 4Cx^2$ and rotating with angular speed ω (see figure). The value of ω is (neglect friction)



(A) $2\sqrt{2gC}$ (B) $\sqrt{\frac{2g}{C}}$ (C) $2\sqrt{gC}$ (D) $\sqrt{\frac{2gC}{ab}}$

Ans (A)

Sol. 

$y = 4cx^2$

$\tan\theta = \frac{dy}{dx} = 8cx$

Let particle as at rest then

$mg\sin\theta = mx\omega^2\cos\theta$

$\Rightarrow g\tan\theta = x\omega^2$

$\Rightarrow g \times (8cx) = x\omega^2$

$\omega^2 = \sqrt{8gc}$

$\omega^2 = 2\sqrt{2gc}$

6. An amplitude modulated wave is represented by expression $v_m = 5(1 + 0.6\cos 6280t)\sin(211 \times 10^4 t)$ volts. The minimum and maximum amplitudes of the amplitude modeulated wave are, respectively :

(A) $\frac{3}{2}V, 5V$ (B) $3V, 5V$ (C) $\frac{5}{2}V, 8V$ (D) $5V, 8V$

Ans. Offical answer by NTA is (C)

Matrix answer Vmax = 8 and Vmin = 2

Sol. $V_m = 5(1 + 0.6\cos 6280t)\sin(211 \times 10^4 t)$

$= (5 + 3\cos 6280t)\sin(211 \times 10^4 t)$

$V_{max} = 5 + 3 = 8V$

$V_{min} = 5 - 3 = 2V$

7. A beam of protons with speed $4 \times 10^5\ ms^{-1}$ enters a uniform magnetic field of 0.3 T at an angle of 60° to the magnetic field. The pitch of the resulting helical path of protons is close to : (Mass of the proton = 1.67×10^{-27} kg, charge of the proton = 1.69×10^{-19} C)

(A) 12 cm (B) 5 cm (C) 4 cm (D) 2 cm

Ans (C)

Sol. Pitch = (V cos θ) T

$$= (V\cos 60)\left(\frac{2\pi m}{eB}\right)$$

$$= \left(4\times10^{5}\times\frac{1}{2}\right)\left(\frac{2\times3.14\times1.67\times10^{-27}}{1.69\times10^{-19}\times0.3}\right)$$

$$= 4.13\times10^{-2}\,\text{m}$$

$$\approx 4\text{cm}$$

8. The mass density of a spherical galaxy varies as $\frac{K}{r}$ over a large distance 'r' from its centre. In that region, a small star is in a circular orbit of radius R. Then the period of revolution, T depends on R as :

(A) $T^2 \propto R^3$ (B) $T \propto R$ (C) $T^2 \propto R$ (D) $T^2 \propto \frac{1}{R^3}$

Ans (C)

Sol. mass of star is $M = \int_0^R \rho dV$

$$= \int_0^R \frac{K}{r}(4\pi r^2 dr) = 2\pi K R^2$$

gravitation force act as centripetal force for circular motion so

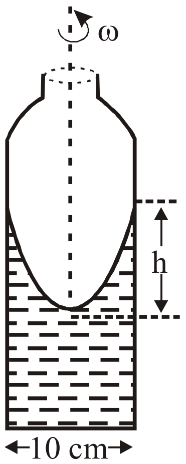
$$\frac{GMm}{R^2} = m\omega^2 R$$

$$\frac{G(2\pi KR^2)}{R^2} = \omega^2 R$$

$$\omega = \sqrt{\frac{2\pi KG}{R}}$$

$$T \propto \frac{1}{\omega} \Rightarrow T \propto R^{\frac{1}{2}}$$

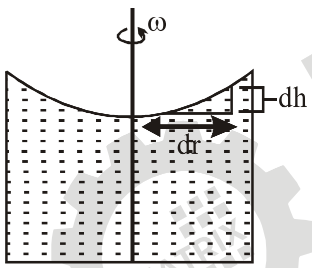
9. A cylindrical vessel containing a liquid is rotated about its axis so that the liquid rises at its sides as shown in the figure. The radius of vessel is 5 cm and the angular speed of rotation is ω rad s^{-1}. The difference in the height, h (in cm) of liquid at the centre of vessel and at the side will be :



(A) $\frac{5\omega^2}{2g}$ (B) $\frac{2\omega^2}{25g}$ (C) $\frac{25\omega^2}{2g}$ (D) $\frac{2\omega^2}{5g}$

Ans (C)

Sol. Pressure is at A same from Horizontal & Vertical side.



$\rho dr\omega^2 r = \rho g dh$

$\omega^2 \int_0^R r dr = g\int_0^h dh$

$\frac{\omega^2 R^2}{2} = gh$

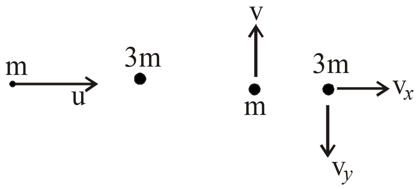
$h = \frac{\omega^2 R^2}{2g} \quad = \frac{\omega^2 25}{2g}$

10. A particle of mass m with an initial velocity $u\hat{i}$ collides perfectly elastically with a mass 3m at rest. It moves with a velocity $v\hat{j}$ after collision, then v is given by :

(A) $v = \frac{1}{16}u$ (B) $v = \frac{u}{\sqrt{2}}$ (C) $v = \sqrt{\frac{2}{3}}u$ (D) $v = \frac{u}{\sqrt{3}}$

Ans (B)

Sol.



Momentum Conservation in x & y

x-direction

$mu + 0 = 0 + 3mv_x$

$\Rightarrow v_x = u/3$

y-direction

$0 = mv - 2mv_y$

$\Rightarrow v = 3v_y$

also $k_i = k_f$ (as collision is elastic)

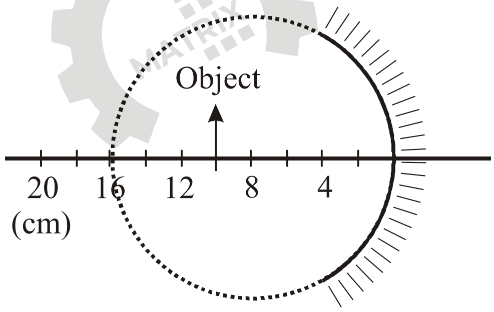
$$\frac{1}{2}mu^2 = \frac{1}{2}mv^2 + \frac{1}{2}3m(v_x^2 + v_y^2)$$

$$\Rightarrow u^2 = v^2 + 3\left[\frac{u^2}{9} + \frac{v^2}{9}\right]$$

$$\Rightarrow u^2 = v^2 + \frac{u^2}{3} + \frac{v^2}{3} \quad \Rightarrow \frac{2}{3}u^2 = \frac{4}{3}v^2$$

$$\Rightarrow u = \sqrt{2}v$$

11.



A spherical mirror is obtained as shown in the figure from a hollow glass sphere. If an object positioned in front of the mirror, what will be the nature and magnification of the image of the object? (Figure drawn as schematic and not to scale)

(A) Erect, virtual and unmagnified

(B) Erect, virtual and magnified

(C) Inverted, real and magnified

(D) Inverted, real and unmagnified

Ans Offical answer by NTA is (C)

Offical answer by Matrix is (D)

Sol. $u = -10$ $R = 8 \Rightarrow f = -4$

$$\frac{1}{V} + \frac{1}{-10} = \frac{1}{-4}$$

$$\Rightarrow \frac{1}{V} = \frac{-1}{4} + \frac{1}{10} = \frac{-3}{20}$$

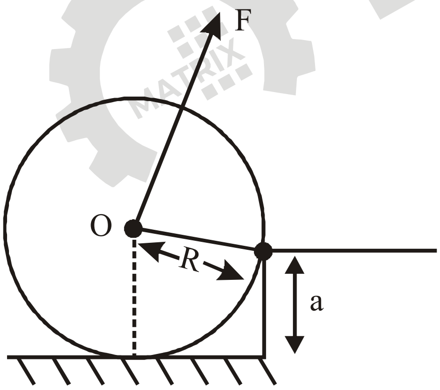
$$V = \frac{-20}{3} =$$

$$m = -\frac{V}{\mu} = -\frac{(-20/3)}{-10} = -\frac{2}{3} = \frac{h_I}{H_o}$$

$$h_0 = -\frac{2}{3}h_I$$

Real inverted and unmagnified

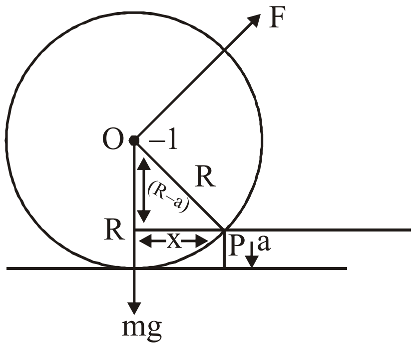
12. A uniform cylinder of mass M and radius R is to be pulled over a step of height a (A < R) by applying a force F at its centre 'O' perpendicular to the plane through the axes of the cylinder on the edge of the step (see figure). The minimum value of F required is :



(A) $Mg\sqrt{\left(\frac{R}{R-a}\right)^2 - 1}$ (B) $Mg\sqrt{1-\left(\frac{R-a}{R}\right)^2}$

(C) $Mg\sqrt{1-\frac{a^2}{R^2}}$ (D) $Mg\frac{a}{R}$

Ans (B)

Sol. 

For minimum value of F, the force F will be perpendicular to the line OP

$x^2 + (R - a)^2 = R$

$x^2 = R^2 - R^2 - a^2 + 2Ra$

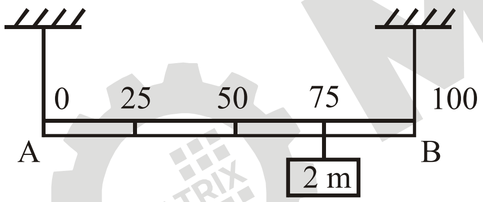
$x = \sqrt{2Ra - a^2}$

$\tau_P = 0$

$\Rightarrow FR = mg\ x$

$\Rightarrow F_{min} = \frac{mg}{R}.x$

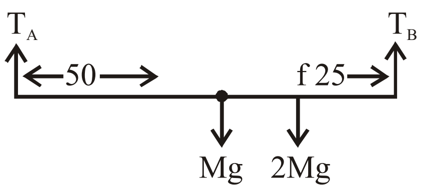
$\Rightarrow F_{min} = \frac{mg}{R}\sqrt{2Ra - a^2}$

13. 

Shown in the figure is rigid and uniform one meter long rod AB held in horizontal position by two strings tied to its ends and attached to the ceiling. The rod is of mass 'm' and has another weight of mass 2 m hung at a distance of 75 cm from A. The tension in the string at A is :

(A) 2 mg (B) 0.75 mg (C) 1 mg (D) 0.5 mg

Ans (C)

Sol. 

From rotational eq. $\tau_B = 0$

$T_A (100) = (mg)50+(2mg)25$

$4T_A = 2mg + 2\ mg$

$T_A = mg$

14. A gas mixture consists of 3 moles of oxygen and 5 moles of argon at temperarture T. Assuming the gases to be ideal and the oxygen bond to be rigid, the total internal energy (in units of RT) of the mixture is :

(A) 20 (B) 13 (C) 15 (D) 11

Ans (C)

Sol. $U = \frac{f_1}{2}n_1RT + \frac{f_2}{2}n_2RT$

$= \frac{5}{2}(3)(R)T + \frac{3}{2}(5)RT$

$= 15RT$

15. A plane electromagnetic wave, has frequency of 2.0×10^{10} Hz its energy density is $1.02 \times 10^{-8} J/m^3$ in vacuum. The amplitude of the magnetic field of the wave is close to ($\frac{1}{4\pi \in_0} = 9 \times 10^9 \frac{Nm^2}{C^2}$ and speed of light = $3 \times 10^8\ ms^{-1}$) :

(A) 180 nT (B) 160 nT (C) 150 nT (D) 190 nT

Ans (B)

Sol. $< U_{EM} > = \frac{1}{2}\frac{{B_o}^2}{\mu_o}$

$1.02 \times 10^{-8} = \frac{1}{2} \times \frac{{B_O}^2}{4\pi \times 10^{-7}}$

$B_O = 16 \times 10^{-8} T$

$= 160\, nT$

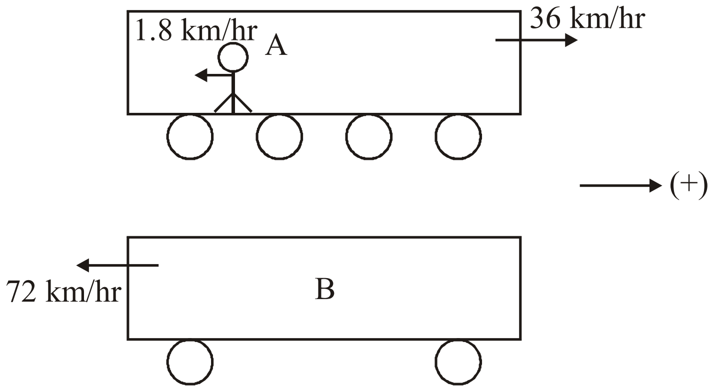
16. Train A and train B are running on parallel tracks in the opposite directions with speeds of 36 km/hour and 72 km/hour, respectively. A person is walking in train A in the direction opposite to its motion with a speed of 1.8 km/hour. Speed (in ms^{-1}) of this person as observed from train B will be close to : (take

the distance between the tracks as negligible)

(A) 31.5 ms^{-1} (B) 29.5 ms^{-1} (C) 28.5 ms^{-1} (D) 30.5 ms^{-1}

Ans (B)

Sol.



$V_A = 36$ km/hr = 10 m/s
$V_B = -72$ km/hr = – 20 m/s
$V_{MA} = -1.8$ km/hr = – 0.5 m/s
$V_{man, B} = V_{man, A} + V_{A, B}$
$= V_{man, A} + V_A - V_B$
$= -0.5 + 10 - (-20)$
$= -0.5 + 30$

= 29.5 m/s

17. Consider four conducting materials copper, tungsten, mercury and aluminium with resistivity ρ_C, ρ_T, ρ_M, and ρ_A respectively. Then :

(A) $\rho_A > \rho_M > \rho_C$ (B) $\rho_A > \rho_T > \rho_C$ (C) $\rho_M > \rho_A > \rho_C$ (D) $\rho_C > \rho_A > \rho_T$

Ans (C)

Sol. This is a fact based question

$\rho_M > \rho_T > \rho_A > \rho_C$

18. In a reactor, 2 kg of $_{92}U^{235}$ fuel is fully used up in 30 days. The energy released per fission is 200 MeV. Given that the Avogadro number, N = 6.023 × 10^{26} per kilo mole and 1 eV = 1.6 × 10^{-19} J. The power output of the reactor is close to :

(A) 54 MW (B) 60 MW (C) 125 MW (D) 35 MW

Ans (B)

Sol. Power = $\frac{\text{energy}}{\text{time}}$

Power = $\frac{\frac{2}{235}\times 6.023\times 10^{26}\times 200\times 1.6\times 10^{-19}}{30\times 24\times 60\times 60}$

= 60 MW

19. The least count of the main scale of a vernier callipers is 1 mm. Its vernier scale is divided into 10 divisions and coincide with 9 divisions of the main scale. When jaws are touching each other, the 7^{th} division of vernier scale coincides with a division of main scale and the zero of vernier scale is lying right side of the zero of main scale. When this vernier is used to measure length of a cylinder the zero of the vernier scaler between 3.1 cm and 3.2 cm and 4^{th} VSD coincides with a main scale division. The length of the cylinder is : (VSD is vernier scale division)

(A) 3.07 cm (B) 2.99 cm (C) 3.21 cm (D) 3.2 cm

Ans (A)

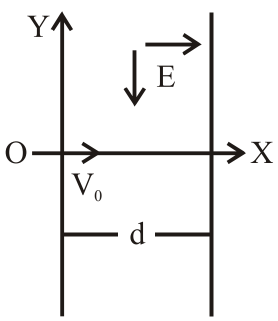
Sol. least count = 1 mm = 0.01 cm

zero error = 0 + 0.01 × 7 = 0.07 cm

Reading = 3.1 + (0.01×4) -0.07

= 3.07 cm

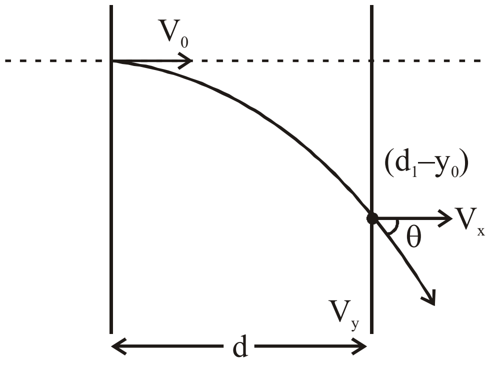
20. A charged particle (mass m and charger q) moves along X axis with velocity V_0. When it passes through the origin it enters a region having uniform electric field $\vec{E} = -E\hat{j}$ which extends upto x = d. Equation of path of electron in the region x > d is :



(A) $y=\frac{qEd}{mV_0^2}(x-d)$ (B) $y=\frac{qEd}{mV_0^2}x$ (C) $y=\frac{qEd^2}{mV_0^2}x$ (D) $y=\frac{qEd}{mV_0^2}\left(\frac{d}{2}-x\right)$

Ans (D)

Sol.



$a_x = 0$ so $V_x = V_0$

and time to come out from field = $\frac{d}{V_0}$

$a_y = \frac{qE}{m}$ $V_y = \left(\frac{qE}{m}\right)\left(\frac{d}{V_0}\right)$

$V_y = \frac{qEd}{mV_0}$

$\tan\theta = \frac{V_y}{V_x} = \frac{\frac{qEd}{mV_0}}{V_0} = \frac{qEd}{mV_0^2}$

tan θ is slope of St. line on which particle will move. Particle move on St. line, when particle comes out from field because there is no force.

So we have to find eq. of St. line having slope $\left(-\frac{qEd}{mV_0^2}\right)$ and passing through a point (d, – y_0)

where $y_0 = \frac{1}{2}\left(\frac{qE}{m}\right)\frac{d^2}{V_0^2}$

$y = MX + C$ (d, $-y_0$)

$-y_0 = Md + C$ $\Rightarrow C = -y_0 - Md$

$= -\frac{1}{2}\frac{qEd^2}{mV_0^2} + \frac{qEd^2}{mV_0^2}$

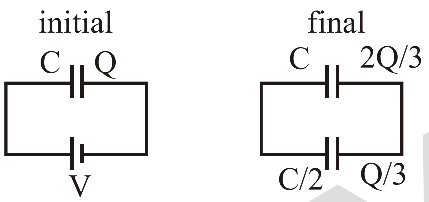
$$C = \frac{qEd^2}{2mV_0^2}$$

$$y = \frac{qEd^2}{mV_0^2}x + \frac{qEd^2}{2mV_0^2} = \frac{qEd}{mV_0^2}\left[\frac{d}{2} - X\right]$$

21. A 5 μ F capacitor is charged fully by a 220 V supply. It is then disconnected from the supply and is connected in series to another uncharged 2.5 μF capacitor. If the energy change during the charge redistribution is $\frac{X}{100}$ J then value of X to the nearest integer is _______.

Ans Offical answer by NTA is 36

Matrix answer is 4

Sol. 

$Q = CV$

$$U_i = \frac{1}{2}CV^2$$

$$U_f = \frac{2}{9}CV^2 + \frac{CV^2}{9} = \frac{CV^2}{3}$$

$$\Delta H = U_i - U_f = \frac{1}{2}CV^2 - \frac{CV^2}{3} = \frac{CV^2}{6}$$

$$\Delta H = \frac{5\times10^{-6}\times220\times220}{6} = \frac{X}{100}$$

$X \approx 4$

22. An engine takes in 5 moles of air at 20°C and 1 atm, and compresses it adiabaticaly to $1/10^{th}$ of the original volume. Assuming air to be a diatomic ideal gas made up of rigid molecules, the change in its internal energy during this process comes out to be X KJ. The value of X to the nearest integer is _____.

Ans 4

Sol. For adiabatic process TV^{r-1} = constant

$$T_1V^{r-1} = T_2\left(\frac{V}{10}\right)^{r-1}$$

$$(293)\,V^{\frac{7}{5}-1} = T_2\left(\frac{V}{10}\right)^{\frac{7}{5}-1}$$

$$293\left(10^{2/5}\right) = T_2$$

$$\Delta U = \frac{f}{2}nR\Delta T$$

$$= \frac{5}{2}\times.5\times\frac{25}{3}\times(T_2 - 293)$$

$$= \frac{5}{2}\times 5\times\frac{25}{3}\times\left[293(10)^{2/5} - 293\right]$$

$$= \frac{5}{2}\times 5\times\frac{25}{3}\times 293\left[10^{2/5} - 1\right]$$

$\approx 4KJ$

23. A circular coil of radius 10 cm is placed in a uniform magnetic field of 3.0×10^{-5} T with its plane perpendicular to the field initially. It is rotated at constant angular speed about an axis along the diameter of coil and perpendicular to magnetic field so that it undergoes half of rotation in 0.2s. The maximum value of EMF induced (in μV) in the coil will be close to the integer ______.

Ans 15

Sol. $\phi = B.A = BA\cos\omega t$

$$\varepsilon mf = \frac{-d\theta}{dt} = \omega BA\sin\omega t$$

$$(emf)_{max} = \omega BA$$

$$\frac{T}{2} = 0.2$$

$$T = 0.4 = \frac{2\pi}{\omega} \Rightarrow \omega = \frac{\pi}{0.2}$$

$$(emf)_{max} = B\omega A = \frac{3\times10^{-5}\times\pi(10\times10^{-2})^2\pi}{0.2} \approx 15\times10^{-6}V \approx 15\mu V$$

24. When radiation of wavelength λ is used too illuminate a metallic surface, the stopping potential is V. When the same surface is illuminated with radiation of wavelength 3λ the stopping potential is $\frac{V}{4}$. If the threshold wavelength for the metallic surface is $n\lambda$ then value of n will be ______.

Ans 9

Sol. $\frac{hc}{\lambda} = \phi + eV$ .... (1)

$\frac{hc}{3\lambda} = \phi + \frac{eV}{4}$ .... (2)

from (1) & (2)

$\frac{hc}{\lambda}\left(1 - \frac{1}{3}\right) = \frac{3}{4}eV$

$\frac{hc}{\lambda}\frac{2}{3} = \frac{3}{4}eV$

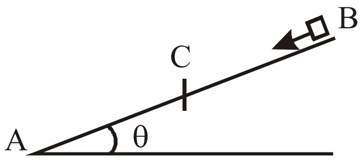
$eV = \frac{8}{9}\frac{hc}{\lambda}$

$\frac{hc}{\lambda} = \phi + \frac{8}{9}\frac{hc}{\lambda}$

$\phi = \frac{hc}{9\lambda} = \frac{hc}{\lambda_{th}}$

$\lambda_{th} = 9\lambda$

$\therefore k = 9$

25. 

A small block starts slipping down from a point B on an inclined plane AB, which is making an angle θ with the horizontal section BC is smooth and the remaining section CA is rough with a coefficient of friction μ. It is found that the block comes to rest as it reaches the bottom (point A) of the inclined plane. If BC = 2AC, the coefficient of friction is given by $\mu = k \tan\theta$. the value of k is _______.

Ans 3

Sol. Let $AC = d$ then $BC = 2d$

from work – energy theorem

$Mg(3d \sin\theta) - \mu Mg \cos\theta(d) = 0 - 0$

$3 \sin\theta = \mu \cos\theta \Rightarrow \mu = 3\tan\theta \Rightarrow K = 3$