

JEE Adv. June 2023
Question Paper With Text Solution
04 June | Paper-1

PHYSICS



JEE Main & Advanced | XI-XII Foundation | VI-X Pre-Foundation

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**SECTION 1 (Maximum Marks: 12)**

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 **ONLY** if (all) the correct option(s) is(are) chosen;

Partial Marks : +3 If all the four options are correct but **ONLY** three options are chosen;

Partial Marks : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;

Partial Marks : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

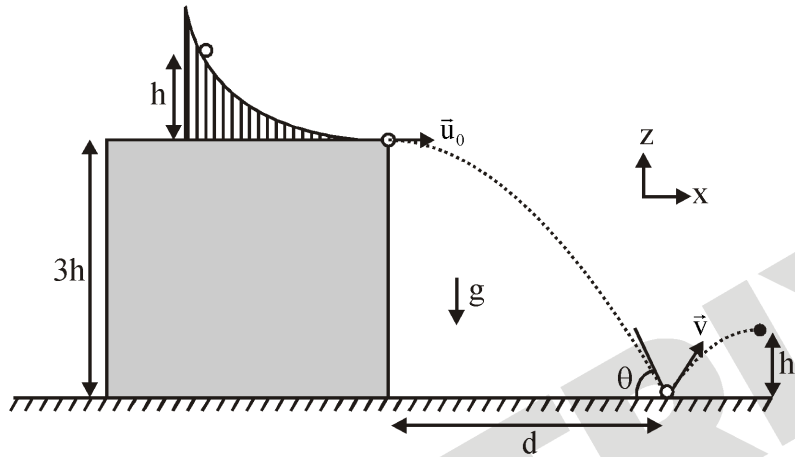
Negative Marks : -2 In all other cases.

- For example, in a question, if (A), (B) and (D) are the **ONLY** three options corresponding to correct answers, then
 - choosing **ONLY** (A), (B) and (D) will get +4 marks;
 - choosing **ONLY** (A) and (B) will get +2 marks;
 - choosing **ONLY** (A) and (D) will get +2 marks;
 - choosing **ONLY** (B) and (D) will get +2 marks;
 - choosing **ONLY** (A) will get +1 mark;
 - choosing **ONLY** (B) will get +1 mark;
 - choosing **ONLY** (D) will get +1 mark;
 - choosing no option (i.e. the question is unanswered) will get 0 marks; and
 - choosing any other combination of options will get -2 marks.

1. A slide with a frictionless curved surface, which becomes horizontal at its lower end, is fixed on the terrace of a building of height $3h$ from the ground, as shown in the figure. A spherical ball of mass m is released on the slide from rest at a height h from the top of the terrace. The ball leaves the slide with a velocity $\vec{u}_0 = u_0 \hat{x}$ and falls on



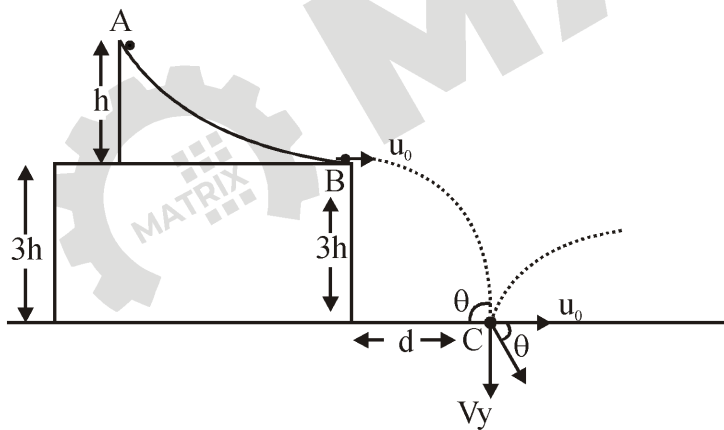
the ground at a distance d from the building making an angle θ with the horizontal. It bounces off with a velocity \vec{v} and reaches a maximum height h_1 . The acceleration due to gravity is g and the coefficient of restitution of the ground is $1/\sqrt{3}$. Which of the following statement(s) is(are) correct?



- (A) $\vec{u}_0 = \sqrt{2gh} \hat{x}$ (B) $\vec{v} = \sqrt{2gh} (\hat{x} - \hat{z})$ (C) $\theta = 60^\circ$ (D) $d/h_1 = 2\sqrt{3}$

Ans. ACD

Sol.



For A to B: $\omega_{\text{net}} = \Delta K$

$$\Rightarrow mgh = \frac{1}{2} mu_0^2$$

$$\Rightarrow u_0 = \sqrt{2gh} \quad (\text{i})$$

For B to C:

$$\text{time of flight (T)} = \sqrt{\frac{2 \times 3h}{g}} = \sqrt{\frac{6h}{g}}$$

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$$d = u_0 \times \sqrt{\frac{6h}{g}}$$

$$d = \sqrt{2gh} \sqrt{\frac{6h}{g}} = \sqrt{12}h$$

$$d = 2\sqrt{3}h$$

At C:

$$u_x = u_0 = \sqrt{2gh}$$

$$\& v_z^2 = 0 + 2 \times g \times 3h$$

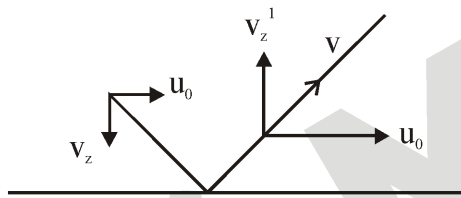
$$v_z = \sqrt{6gh}$$

$$\tan \theta = \frac{v_z}{u_x} = \frac{\sqrt{6gh}}{\sqrt{2gh}}$$

$$\tan \theta = \sqrt{3}$$

$$\theta = 60^\circ$$

At C:



In vertical direction

$$v_z^1 = ev_z = \frac{1}{\sqrt{3}} \sqrt{6gh}$$

$$v_z^1 = \sqrt{2gh} \Rightarrow h_1 = \frac{(v_z^1)^2}{2g} = h \Rightarrow \frac{d}{h_1} = \frac{d}{h} = 2\sqrt{3}$$

So velocity after collision

$$\vec{v} = \sqrt{2gh}(\hat{i}) + \sqrt{2gh}(\hat{k})$$

2. A plane polarized blue light ray is incident on a prism such that there is no reflection from the surface of the prism. The angle of deviation of the emergent ray is $\delta = 60^\circ$ (see Figure-1). The angle of minimum deviation for red light from the same prism is $\delta_{\min} = 30^\circ$ (see Figure-2). The refractive index of the prism material for blue light is $\sqrt{3}$. Which of the following statement(s) is(are) correct?

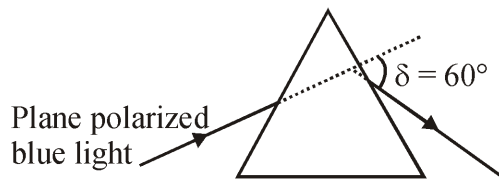


Figure-1

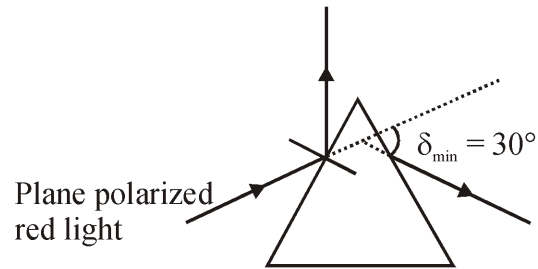
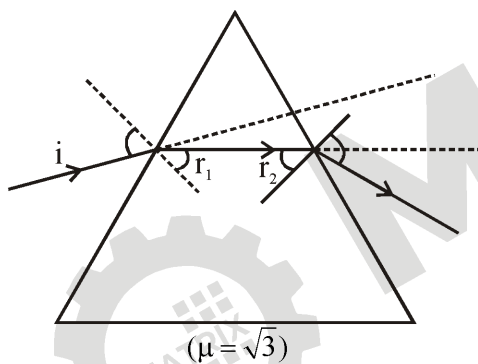


Figure-2

- (A) The blue light is polarized in the plane of incidence.
 (B) The angle of the prism is 45° .
 (C) The refractive index of the material of the prism for red light is $\sqrt{2}$.
 (D) The angle of refraction for blue light in air at the exit plane of the prism is 60° .

Ans. ACD

Sol. $\delta_{\text{blue}} = 60^\circ$ $(\delta_{\text{min}})_{\text{red}} = 30^\circ$



for blue
 angle of incidence = Brewster's angle

$$\tan i = \tan \theta_b = \sqrt{3}$$

$$\boxed{i = 60^\circ}$$

Now

$$1 \times \sin 60^\circ = \sqrt{3} \times \sin r_1$$

$$\Rightarrow \sin r_1 = \frac{1}{2}$$

$$\boxed{r_1 = 30^\circ}$$

$$\text{also } \delta = 60^\circ = 60^\circ + e - A$$

$$\Rightarrow \boxed{e = A}$$

$$\text{also } r_2 = A - r_1 = A - 30^\circ$$

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$$\& \sqrt{3} \times \sin r_2 = 1 \times \sin e$$

$$\Rightarrow \sqrt{3} \sin(A - 30^\circ) = \sin A$$

$$\Rightarrow \sqrt{3} \times [\sin A \cos 30^\circ - \cos A \sin 30^\circ] = \sin A$$

$$\Rightarrow \sqrt{3} \times \frac{\sqrt{3}}{2} \sin A = \sqrt{3} \cos A \times \frac{1}{2} + \sin A$$

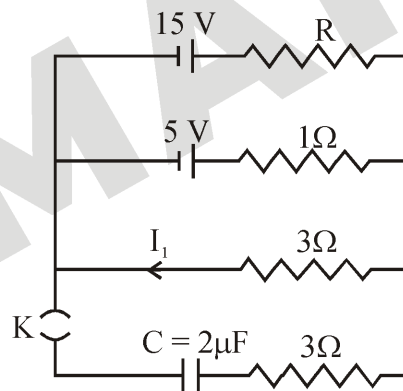
$$\Rightarrow \frac{\sin A}{2} = \frac{\sqrt{3} \cos A}{2}$$

$$\Rightarrow \tan A = \sqrt{3}$$

$$\boxed{A = 60^\circ} \& \boxed{e = 60^\circ}$$

3. In a circuit shown in the figure, the capacitor C is initially uncharged and the key K is open. In this condition, a current of 1 A flows through the $1\ \Omega$ resistor. The key is closed at time $t = t_0$. Which of the following statement(s) is(are) correct?

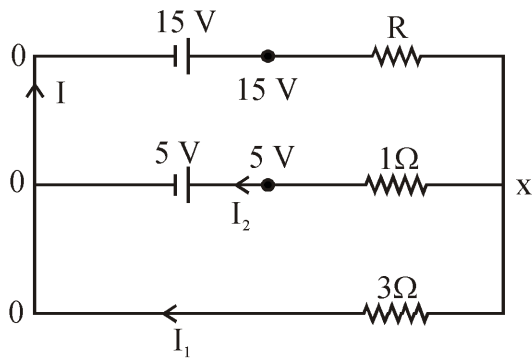
[Given: $e^{-1} = 0.36$]



- (A) The value of the resistance R is $3\ \Omega$.
 (B) For $t < t_0$, the value of current I_1 is 2 A .
 (C) At $t = t_0 + 7.2\ \mu\text{s}$, the current in the capacitor is 0.6 A .
 (D) For $t \rightarrow \infty$, the charge on the capacitor is $12\ \mu\text{C}$.

Ans. ABCD

Sol. at $t = 0$:



$$I_2 = 1A$$

$$\frac{x-5}{1} = 1$$

$$x = 6V$$

$$I_1 = \frac{6-0}{3} = 2A \quad \& \quad I = I_1 + I_2$$

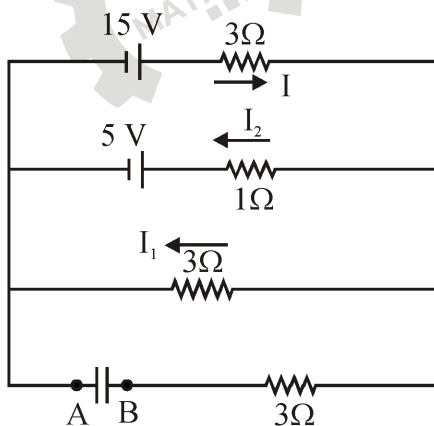
$$I = 2 + 1$$

$$I = 3A$$

$$\text{So } \frac{15-6}{R} = I = 3$$

$$45 \times \frac{400}{1000} \text{ W}$$

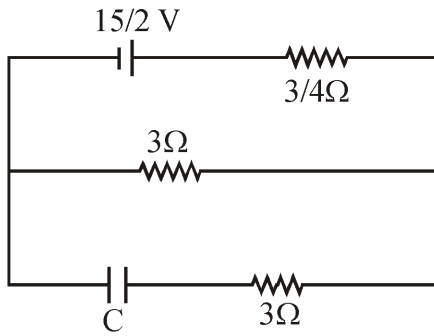
At $t = \infty$:



$$\text{P.D. across AB} = I_1 \times 3 = 2 \times 3 = 6 \text{ V}$$

$$\text{charge on capacitor} = 6 \times 2 = 12\mu\text{c}$$

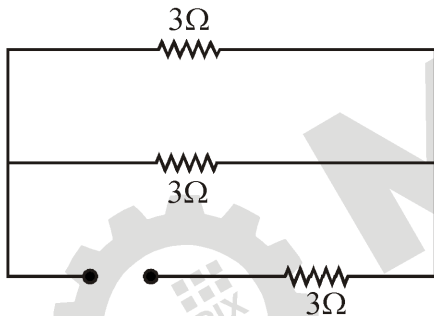
At any time 't':



$$E_{\text{eq}} = \frac{\frac{15}{3} + \frac{5}{1}}{\frac{1}{3} + \frac{1}{1}} = \frac{5+5}{\left(\frac{4}{3}\right)} = \frac{30}{4} = \frac{15}{2} \text{ V}$$

$$r_{\text{eq}} = \frac{3 \times 1}{3+1} = \frac{3}{4} \Omega$$

Using thevenin method

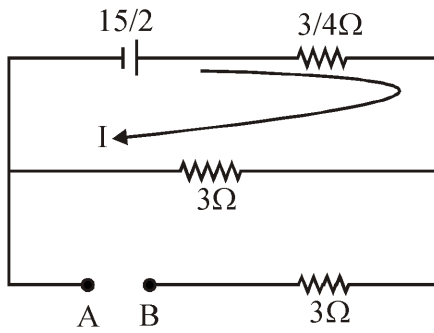


$$R_{\text{eq}} = \frac{\frac{3}{4} \times 3}{\frac{3}{4} + 3} + 3$$

$$R_{\text{eq}} = \frac{\frac{9}{4}}{\left(\frac{15}{4}\right)} + 3$$

$$R_{\text{eq}} = \frac{3}{5} + 3$$

$$R_{\text{eq}} = \frac{18}{5} \Omega$$

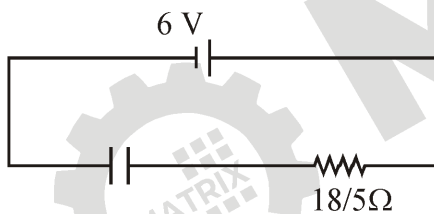


$$I = \frac{\frac{15}{2}}{\left(3 + \frac{3}{4}\right)}$$

$$I = \frac{\left(\frac{15}{2}\right)}{\left(\frac{15}{4}\right)}$$

$$I = 2 \text{ A}$$

$$V_A - V_B = 3 \times 2 = 6 \text{ V}$$



$$Q = Q_0 [1 - e^{-t/RC}]$$

$$I = \frac{dQ}{dt} = Q_0 [e^{-t/RC}] \left[\frac{1}{RC} \right]$$

$$I = \frac{Q_0}{RC} e^{-t/RC}$$

$$\text{(at } t = t_0 + 7.2 \text{ } \mu\text{s)}$$

$$I = \frac{12}{\left(\frac{18}{5}\right) \times 2} e^{-\frac{7.2}{\frac{18}{5} \times 2}}$$

$$I = \frac{5}{3} e^{-\frac{72 \times 5}{36 \times 10}}$$



$$I = \frac{5}{3} \times e^{-1}$$

$$I = \frac{5}{3} \times 0.36 = I = 5 \times 0.12$$

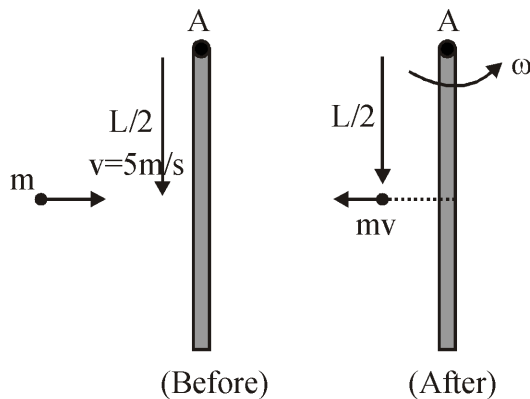
$$I = 0.60 \text{ A}$$

SECTION 2 (Maximum Marks: 12)

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:
 Full Marks : +3 If **ONLY** the correct option is chosen;
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
 Negative Marks : -1 In all other cases.

4. A bar of mass $M = 1.00 \text{ kg}$ and length $L = 0.20 \text{ m}$ is lying on a horizontal frictionless surface. One end of the bar is pivoted at a point about which it is free to rotate. A small mass $m = 0.10 \text{ kg}$ is moving on the same horizontal surface with 5.00 m s^{-1} speed on a path perpendicular to the bar. It hits the bar at a distance $L/2$ from the pivoted end and returns back on the same path with speed v . After this elastic collision, the bar rotates with an angular velocity ω . Which of the following statement is correct?
- (A) $\omega = 6.98 \text{ rad s}^{-1}$ and $v = 4.30 \text{ m s}^{-1}$
 (B) $\omega = 3.75 \text{ rad s}^{-1}$ and $v = 4.30 \text{ m s}^{-1}$
 (C) $\omega = 3.75 \text{ rad s}^{-1}$ and $v = 10.0 \text{ m s}^{-1}$
 (D) $\omega = 6.80 \text{ rad s}^{-1}$ and $v = 4.10 \text{ m s}^{-1}$

Ans. A



Sol.

for system \rightarrow Angular momentum is conserved about A



$$L_i = L_f$$

$$\Rightarrow \left(0.1 \times 5 \times \frac{0.2}{2}\right) = -\left(0.1 \times v \times \frac{0.2}{2}\right) + \frac{1 \times (0.2)^2}{3} \times \omega$$

$$\Rightarrow \frac{5}{2} = \frac{-v}{2} + \frac{2\omega}{3}$$

$$\Rightarrow \boxed{4\omega - 3v = 15} \quad \dots(1)$$

$$\text{and } e = 1 = \frac{\omega \times \frac{0.2}{2} + v}{5}$$

$$v + \frac{\omega}{10} = 5$$

$$\Rightarrow \boxed{10v + \omega = 50} \quad \dots(2)$$

from (1) & (2)

$$40v + 3v = 200 - 15$$

$$\Rightarrow 43v = 185$$

$$v = \frac{185}{43} \Rightarrow v = 4.302 \text{ m/sec}$$

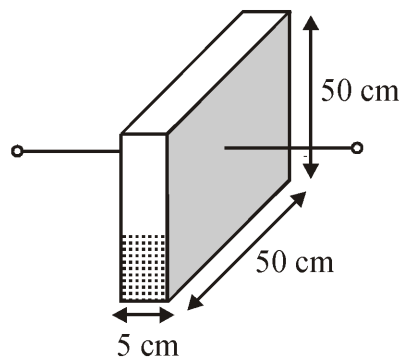
$$\& \omega = 50 - 10 \times 4.302$$

$$\omega = 50 - 43.02$$

$$\omega = 6.98 \text{ rad/sec}$$

5. A container has a base of $50 \text{ cm} \times 50 \text{ cm}$ and height 50 cm , as shown in the figure. It has two parallel electrically conducting walls each of area $50 \text{ cm} \times 50 \text{ cm}$. The remaining walls of the container are thin and non-conducting. The container is being filled with a liquid of dielectric constant 3 at a uniform rate of $250 \text{ cm}^3 \text{ s}^{-1}$. What is the value of the capacitance of the container after 10 seconds?

[Given: Permittivity of free space $\epsilon_0 = 9 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$, the effects of the non-conducting walls on the capacitance are negligible]



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(A) 27 pF

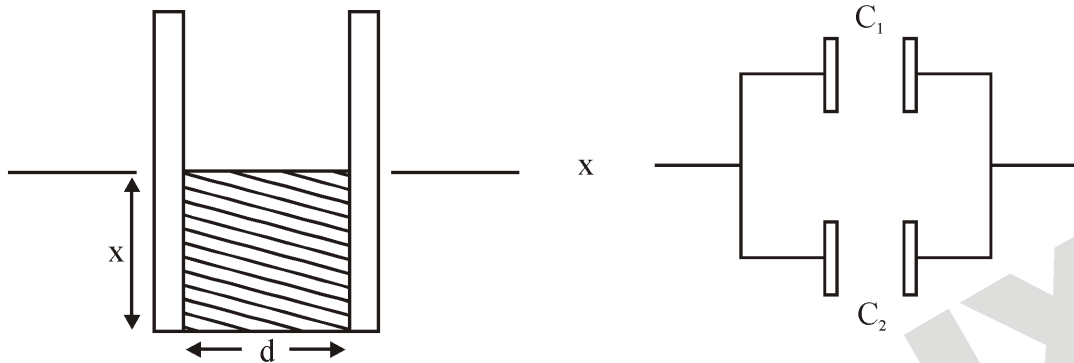
(B) 63 pF

(C) 81 pF

(D) 135 pF

Ans. B

Sol.



in 10 sec

Total volume of dielectric

$$= 250 \times 10$$

$$= 2500 \text{ cm}^3$$

$$\text{So } 50 \times 5 \times x = 2500$$

$$x = \frac{2500}{250}$$

$$x = 10 \text{ cm}$$

$$C_1 = \frac{\epsilon_0 \times A_1}{d}$$

$$C_2 = \frac{\epsilon_r \epsilon_0 \times A_2}{d}$$

$$C_{\text{eq}} = C_1 + C_2$$

$$= \frac{\epsilon_0}{d} [A_1 + \epsilon_r A_2]$$

$$= \frac{9 \times 10^{-12}}{5 \times 10^{-2}} [40 \times 50 + 3 \times 10 \times 50] \times 10^{-4}$$

$$= \frac{9}{5} \times 10^{-14} [2000 + 1500]$$

$$\frac{9}{5} \times 35 \times 10^{-12}$$

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$$= 63 \times 10^{-12} \text{ F}$$

$$= 63 \text{ pF}$$

6. One mole of an ideal gas expands adiabatically from an initial state (T_A, V_0) to final state $(T_f, 5V_0)$. Another mole of the same gas expands isothermally from a different initial state (T_B, T_0) to the same final state $(T_f, 5V_0)$. The ratio of the specific heats at constant pressure and constant volume of this ideal gas is γ . What is the ratio

$$T_A/T_B?$$

(A) $5^{\gamma-1}$

(B) $5^{1-\gamma}$

(C) 5^γ

(D) $5^{1+\gamma}$

Ans. A

Sol. A adiabatic process: $T_A V_0^{\gamma-1} = T_f (5V_0)^{\gamma-1}$ (1)

Isothermal process: $T_B = T_f$ (2)

(1) \div (2)

$$\frac{T_A}{T_B} V_0^{\gamma-1} = (5V_0)^{\gamma-1}$$

$$\frac{T_A}{T_B} = 5^{\gamma-1}$$

7. Two satellites P and Q are moving in different circular orbits around the Earth (radius R). The heights of P and Q from the Earth surface are h_P and h_Q , respectively, where $h_P = R/3$. The accelerations of P and Q due to Earth's gravity are g_P and g_Q , respectively. If $g_P/g_Q = 36/25$, what is the value of h_Q ?

(A) $3R/5$

(B) $R/6$

(C) $6R/5$

(D) $5R/6$

Ans. A

Sol. Satellite P: $h_P = \frac{R}{3}$ & radius of orbit (r_P) = $\frac{R + R}{3} = \frac{4R}{3}$

Satellite Q: h_Q & radius of orbit = r_Q

$$\frac{g_P}{g_Q} = \frac{\frac{GM_e}{r_P^2}}{\frac{GM_e}{r_Q^2}}$$

$$\frac{36}{25} = \frac{r_Q^2}{r_P^2}$$

$$\frac{r_Q}{r_P} = \frac{6}{5}$$



$$r_Q = \frac{6}{5} \times r_P = \frac{6}{5} \times \frac{4R}{3} = \frac{8R}{5}$$

$$h_Q = \frac{8R}{5} - R = \frac{3R}{5}$$

SECTION 3 (Maximum Marks: 24)

- This section contains **SIX (06)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the onscreen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 If **ONLY** the correct integer is entered;

Zero Marks : 0 In all other cases.

8. A Hydrogen-like atom has atomic number Z . Photons emitted in the electronic transitions from level $n = 4$ to level $n = 3$ in these atoms are used to perform photoelectric effect experiment on a target metal. The maximum kinetic energy of the photoelectrons generated is 1.95 eV. If the photoelectric threshold wavelength for the target metal is 310 nm, the value of Z is _____.

[Given: $hc = 1240$ eV-nm and $Rhc = 13.6$ eV, where R is the Rydberg constant, h is the Planck's constant and c is the speed of light in vacuum]

Ans. 3

Sol. In photoelectric effect: $E_{ph} - \phi = K_{max}$

$$13.6 \times Z^2 \left(\frac{1}{3^3} - \frac{1}{4^2} \right) - \frac{hc}{\lambda_{th}} = 1.95$$

$$13.6 Z^2 \times \frac{7}{144} - \frac{1240}{310} = 1.95$$

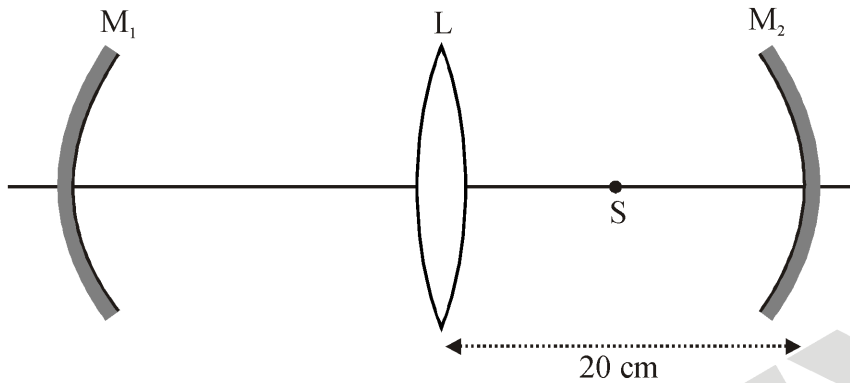
$$Z^2 \times \frac{5.95 \times 144}{13.6 \times 7} = 9$$

$$Z^2 = 3$$

9. An optical arrangement consists of two concave mirrors M_1 and M_2 , and a convex lens L with a common principal axis, as shown in the figure. The focal length of L is 10 cm. The radii of curvature of M_1 and M_2 are 20 cm and 24 cm, respectively. The distance between L and M_2 is 20 cm. A point object S is placed at the mid-

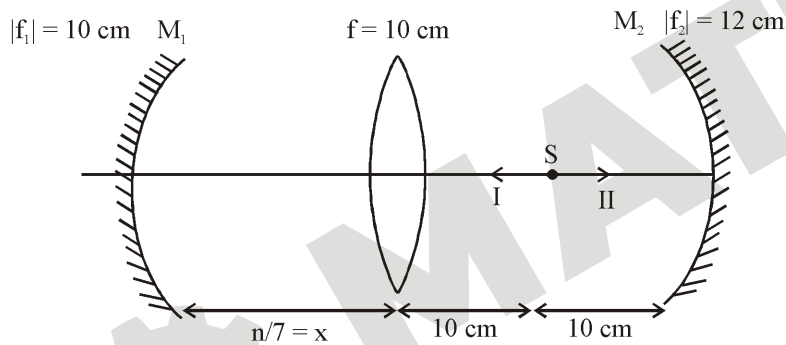


point between L and M_2 on the axis. When the distance between L and M_1 is $n/7$ cm, one of the images coincides with S. The value of n is _____.



Ans. 80 or 150 or 220

Sol.



For I:

1. Image formed by lens is at ∞
2. Image formed by M_1 is at its focus i.e. 10 cm to the right of its pole.
3. Image formed by lens now cannot be at S because for that rays need to be incident parallel to PA.

For II:

1. Image formed by M_2

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f_2}$$

$$v = \frac{uf_2}{u - f_2} = \frac{(-10)(-12)}{2} = 60 \text{ cm} \quad (\text{to the right of pole of } M_2)$$

2. Image formed by lens

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$



$$v = \frac{uf}{u+f} = \frac{(-80)(10)}{-70} = \frac{80}{7} \quad (\text{to the left of lens})$$

3. If the rays coming from lens are incident on pole of M_1 , then they will reflect symmetrically on a mirrored path about PA and after refraction from lens L refraction from mirror M_2 , they will converge at S finally. So,

$$\frac{80}{7} = \frac{n}{7}$$

$$n = 80$$

4. If the rays coming from lens converge onto centre of curvature of M_1 , then they will retrace their path and eventually converge at S.

$$\frac{80}{7} + 20 = \frac{n}{7} \quad \Rightarrow n = 220$$

5. If the rays coming from lens converge onto focus of M_1 , then they will become parallel to principle axis after reflection from M_1 and finally get converged at S because S lies at the focus of lens.

$$\frac{80}{7} + 10 = \frac{n}{7} \quad \Rightarrow n = 150$$

10. In an experiment for determination of the focal length of a thin convex lens, the distance of the object from the lens is 10 ± 0.1 cm and the distance of its real image from the lens is 20 ± 0.2 cm. The error in the determination of focal length of the lens is $n\%$. The value of n is _____.

Ans. 1

Sol.
$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u} \Rightarrow \frac{1}{f} = \frac{1}{20} - \frac{1}{(-10)} \Rightarrow f = \frac{20}{3}$$

$$\frac{\Delta f}{f^2} = \frac{\Delta v}{v^2} + \frac{\Delta u}{u^2}$$

$$\left(\frac{\Delta f}{f}\right) \times \frac{1}{f} = \frac{0.2}{20^2} + \frac{0.1}{10^2}$$

$$\frac{\Delta f}{f} = \left(\frac{0.2}{400} + \frac{0.1}{100}\right) \times \frac{20}{3}$$

$$\frac{\Delta f}{f} = \frac{0.6}{400} \times \frac{20}{3}$$

$$\frac{\Delta f}{f} \times 100 = \frac{4}{400} \times 100 = 1\%$$

11. A closed container contains a homogeneous mixture of two moles of an ideal monatomic gas ($\gamma = 5/3$) and one mole of an ideal diatomic gas ($\gamma = 7/5$). Here, γ is the ratio of the specific heats at constant pressure and constant volume of an ideal gas. The gas mixture does a work of 66 Joule when heated at constant pressure.



The change in its internal energy is _____ Joule.

Ans. 121

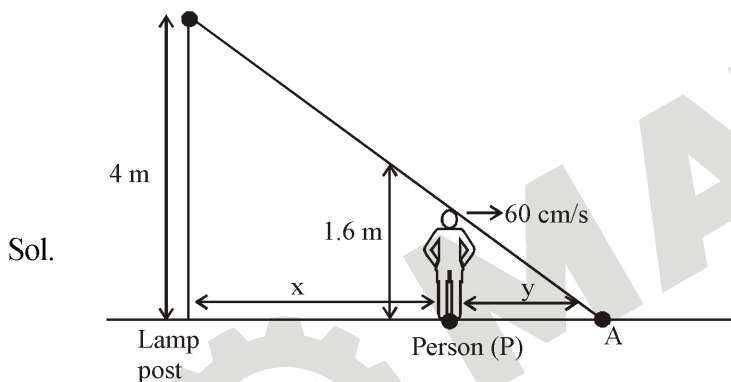
Sol.
$$f_{eq} = \frac{n_1 f_1 + n_2 f_2}{n_1 + n_2} = \frac{2 \times 3 + 1 \times 5}{3} = \frac{11}{3}$$

WD at constant pressure = $P\Delta V$ or $nR\Delta T = 66 \text{ J}$

$$\Delta U = \frac{f_{eq} nR\Delta T}{2} = \frac{11}{3 \times 2} \times 66 = 121 \text{ J}$$

12. A person of height 1.6 m is walking away from a lamp post of height 4 m along a straight path on the flat ground. The lamp post and the person are always perpendicular to the ground. If the speed of the person is 60 cm s^{-1} , the speed of the tip of the person's shadow on the ground with respect to the person is _____ cm s^{-1} .

Ans. 40



$$v_A - v_P = ?$$

$$\frac{4}{x+y} = \frac{1.6}{y}$$

$$4y = 1.6x + 1.6y$$

$$2.4y = 1.6x$$

$$y = \frac{2}{3}x$$

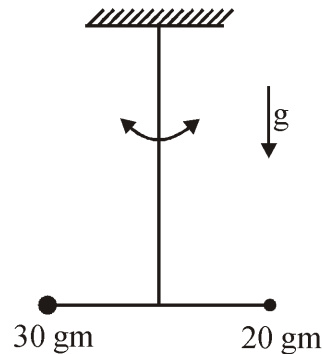
$$\frac{dy}{dt} = \frac{2}{3} \frac{dx}{dt}$$

$$v_A - v_P = \frac{2}{3} \times 60 \text{ cm/s} = 40 \text{ cm/s}$$

13. Two point-like objects of masses 20 gm and 30 gm are fixed at the two ends of a rigid massless rod of length 10 cm. This system is suspended vertically from a rigid ceiling using a thin wire attached to its center of mass,



as shown in the figure. The resulting torsional pendulum undergoes small oscillations. The torsional constant of the wire is $1.2 \times 10^{-8} \text{ N m rad}^{-1}$. The angular frequency of the oscillations in $n \times 10^{-3} \text{ rad s}^{-1}$. The value of n is _____.



Ans. 10

Sol. $\omega = \sqrt{\frac{C}{I}}$

$$I = \frac{m_1 m_2 r^2}{m_1 + m_2} = \frac{20 \times 10^{-3} \times 30 \times 10^{-3} \times 10^{-2}}{20 \times 10^{-3} + 30 \times 10^{-3}}$$

$$\omega = \sqrt{\frac{1.2 \times 10^{-8}}{\frac{600 \times 10^{-5}}{50}}} = \sqrt{\frac{6 \times 10^{-8}}{6 \times 10^{-4}}} = 10^{-2} = 10 \times 10^{-3} \text{ rad/s}$$

SECTION 4 (Maximum Marks: 12)

- This section contains **FOUR (04)** Matching List Sets.
- Each set has **ONE** Multiple Choice Question.
- Each set has **TWO** lists: **List-I** and **List-II**.
- List-I has **Four** entries (P), (Q), (R) and (S) and List-II has Five entries (1), (2), (3), (4) and (5).
- **FOUR** options are given in each Multiple Choice Question based on **List-I** and **List-II** and **ONLY ONE** of these four options satisfies the condition asked in the Multiple Choice Question.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : **+3 ONLY** if the option corresponding to the correct combination is chosen;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

Negative Marks : -1 In all other cases.

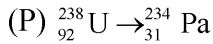
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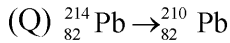
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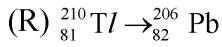
14. List-I shows different radioactive decay processes and List-II provides possible emitted particles. Match each entry in List-I with an appropriate entry from List-II, and choose the correct option.



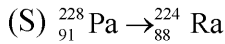
(1) one α particle and one β^+ particle



(2) three β^- particles and one α particle



(3) two β^- particles and one α particle



(4) one α particle and one β^- particle

(5) one α particle and two β^+ particles

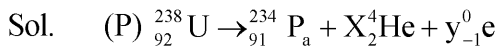
(A) $P \rightarrow 4, Q \rightarrow 3, R \rightarrow 2, S \rightarrow 1$

(B) $P \rightarrow 4, Q \rightarrow 1, R \rightarrow 2, S \rightarrow 5$

(C) $P \rightarrow 5, Q \rightarrow 3, R \rightarrow 1, S \rightarrow 4$

(D) $P \rightarrow 5, Q \rightarrow 1, R \rightarrow 3, S \rightarrow 2$

Ans. A



By mass:

$$238 = 234 + 4x$$

$$\Rightarrow x = 1$$

By charge :

$$92 = 91 + 2x - y$$

$$\Rightarrow y = 1$$

$\therefore P \rightarrow$ option(4)



By mass:

$$214 = 210 + 4x$$

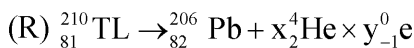
$$\Rightarrow x = 1$$

By charge:

$$82 = 82 + 2 \times -Y$$

$$\Rightarrow Y = 2$$

$\therefore Q \rightarrow$ option(3)



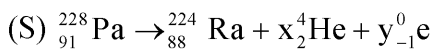
By mass: $210 = 206 + 4x$

$$\Rightarrow x = 1$$

By charge : $81 = 82 + 2x - y$

$$\Rightarrow y = 3$$

$\therefore R \rightarrow$ option (2)



By mass: $228 = 224 + 4x$



$$\Rightarrow x = 1$$

By charge: $91 = 88 + 2x - y$

$$\Rightarrow y = -1$$

Its actually β^+

$\therefore S \rightarrow$ option (1)

15. Match the temperature of a black body given in List-I with an appropriate statement in List-II, and choose the correct option.

[Given: Wien's constant as $2.9 \times 10^{-3} \text{ m-K}$ and $\frac{hc}{e} = 1.24 \times 10^{-6} \text{ V-m}$]

List-I

(P) 2000 K

(Q) 3000 K

(R) 5000 K

(S) 10000 K

(A) P \rightarrow 3, Q \rightarrow 5, R \rightarrow 2, S \rightarrow 3

(C) P \rightarrow 3, Q \rightarrow 4, R \rightarrow 2, S \rightarrow 1

Ans. C

Sol. (P) $T = 2000\text{K}$

$$\lambda = \frac{b}{T} = \frac{2.9 \times 10^{-3}}{2000} = 1.45 \times 10^{-6} = 1450 \text{ nm}$$

Does not fall in visible range

Energy of photon, $E = \frac{hc}{\lambda} = \frac{1.24 \times 10^{-6}}{1.45 \times 10^{-6}} \text{ eV} = 0.855 < 4\text{eV}$

For first minima :

$$\theta = \sin^{-1} \frac{\lambda}{a}$$

$\lambda \uparrow \theta \uparrow$ & $\lambda \propto \frac{1}{T} \Rightarrow$ at lowest temp widest central maxima will be obtained.

among all, 2000K is lowest.

List-II

(1) The radiation at peak wavelength can lead to emission of photoelectrons from a metal of work function 4 eV.

(2) The radiation at peak wavelength is visible to human eye.

(3) The radiation at peak emission wavelength will result in the widest central maximum of a single slit diffraction.

(4) The power emitted per unit area is 1/16 of that emitted by a blackbody at temperature 6000 K.

(5) The radiation at peak emission wavelength can be used to image human bones.

(B) P \rightarrow 3, Q \rightarrow 2, R \rightarrow 4, S \rightarrow 1

(D) P \rightarrow 1, Q \rightarrow 2, R \rightarrow 5, S \rightarrow 3



$\therefore \theta$ is highest

P \rightarrow 3

(Q): T = 3000K

$$\lambda = \frac{b}{T} = \frac{2.9 \times 10^{-3}}{3000} \approx 10^{-6} = 1000 \text{ nm}$$

Does not fall in visible range.

$$\text{Energy of photon : } E = \frac{hc}{\lambda} = \frac{1.24 \times 10^{-6}}{10^{-6}} \text{ eV} = 1.24 \text{ eV} < 4 \text{ eV}$$

$$\frac{P_{3000}}{P_{6000}} = \frac{eA\sigma(3000)^4}{eA\sigma(6000)^4} = \frac{1}{16}$$

Q \rightarrow (4)

(R): T = 5000K

$$\lambda = \frac{b}{T} = \frac{2.9 \times 10^{-3}}{5000} = 0.58 \times 10^{-6} = 580 \text{ nm}$$

it falls under visible region.

R \rightarrow 2

(S) T = 10000

$$\lambda = \frac{b}{T} = \frac{2.9 \times 10^{-3}}{10000} = 2.9 \times 10^{-7} = 290 \text{ nm}$$

does not fall under visible region

$$\text{Energy of photon : } E = \frac{hc}{\lambda} = \frac{1.24 \times 10^{-6}}{2.9 \times 10^{-7}} = 4.2 \text{ eV}$$

This photon can ejecte e^- from metal of $\phi = 4 \text{ eV}$

16. A series LCR circuit is connected to a $45 \sin(\omega t)$ Volt source. The resonant angular frequency of the circuit is 10^5 rad s^{-1} and current amplitude at resonance is I_0 . When the angular frequency of the source is $\omega = 8 \times 10^4 \text{ rad s}^{-1}$, the current amplitude in the circuit is $0.05 I_0$. If $L = 50 \text{ mH}$, match each entry in List-I with an appropriate value from List-II and choose the correct option.

List-I

(P) I_0 in mA

(Q) The quality factor of the circuit

(R) The bandwidth of the circuit in rad s^{-1}

(S) The peak power dissipated at resonance in Watt

List-II

(1) 44.4

(2) 18

(3) 400

(4) 2250



(5) 500

(A) $P \rightarrow 2, Q \rightarrow 3, R \rightarrow 5, S \rightarrow 1$ (B) $P \rightarrow 3, Q \rightarrow 1, R \rightarrow 4, S \rightarrow 2$ (C) $P \rightarrow 4, Q \rightarrow 5, R \rightarrow 3, S \rightarrow 1$ (D) $P \rightarrow 4, Q \rightarrow 2, R \rightarrow 1, S \rightarrow 5$

Ans. B

Sol. $\frac{1}{\sqrt{LC}} = 10^5$

$$I_0 = \frac{45}{R}$$

$$0.05I_0 = \frac{45}{\sqrt{R^2 + \left(0.80 \times X_{L_0} - \frac{5}{4} X_{C_0}\right)^2}}$$

Where $X_{L_0} = X_{C_0}$ are at resonant frequencies

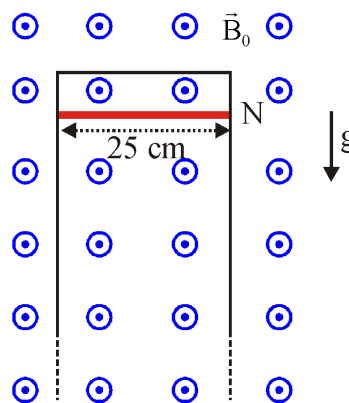
On solving, $R \approx \frac{450 \Omega}{4} \Rightarrow I_0 \approx 400 \text{ mA}$

Quality factor $Q = \frac{1}{R} \sqrt{\frac{L}{C}} \approx 44.44$

$$Q = \frac{\omega_0}{\Delta\omega} \Rightarrow \Delta\omega \approx 2250 \text{ rad/s}$$

Peak power = $45 \times \frac{400}{1000} \text{ W} = 18$

17. A thin conducting rod MN of mass 20 gm, length 25 cm and resistance 10Ω is held on frictionless, long, perfectly conducting vertical rails as shown in the figure. There is a uniform magnetic field $B_0 = 4 \text{ T}$ directed perpendicular to the plane of the rod-rail arrangement. The rod is released from rest at time $t = 0$ and it moves down along the rails. Assume air drag is negligible. Match each quantity in List-I with an appropriate value from List-II, and choose the correct option.

[Given: The acceleration due to gravity $g = 10 \text{ m s}^{-2}$ and $e^{-1} = 0.4$]**MATRIX JEE ACADEMY**

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List-I

- (P) At $t = 0.2$ s, the magnitude of the induced emf in Volt
 (Q) At $t = 0.2$ s, the magnitude of the magnetic force in Newton
 (R) At $t = 0.2$ s, the power dissipated as heat in Watt
 (S) The magnitude of terminal velocity of the rod in m s^{-1}

List-II

- (1) 0.07
 (2) 0.14
 (3) 1.20
 (4) 0.12
 (5) 2.00

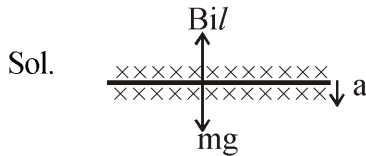
(A) $P \rightarrow 5, Q \rightarrow 2, R \rightarrow 3, S \rightarrow 1$

(B) $P \rightarrow 3, Q \rightarrow 1, R \rightarrow 4, S \rightarrow 5$

(C) $P \rightarrow 4, Q \rightarrow 3, R \rightarrow 1, S \rightarrow 2$

(D) $P \rightarrow 3, Q \rightarrow 4, R \rightarrow 2, S \rightarrow 5$

Ans. D



$$mg - i\ell B = ma$$

$$i = \frac{B\ell v}{R}$$

$$mg - \frac{B^2 \ell^2}{R} v = \frac{mdv}{dt}$$

$$\frac{dv}{dt} = g - \frac{B^2 \ell^2}{mR} v = g - cv$$

$$\text{where } c = \frac{B^2 \ell^2}{mR} = 5$$

$$v = 2(1 - e^{-5t})$$

$$\text{at } t = 0.2 \Rightarrow v = 1.20$$

$$\text{at } t = 0.2 \Rightarrow F_m = 0.12$$

$$P = i^2 R = 0.14$$

$$v_{\text{terminal}} = 2$$

$$(p) \rightarrow 3, (q) \rightarrow 4, (r) \rightarrow 2, (s) \rightarrow 5$$